

Modeling of energy storage materials

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Outline

1. Motivation to study energy materials and introduction into battery components

2. Modeling of solid electrodes

3. Modeling of electrolytes and interfaces

4. High-throughput modeling

5. Few examples from our experience: OH defects in LiFePO_4 , antisite defects in layered oxides, migration barriers in cathodes

More than **1 billion gasoline cars** on Earth



Gas chamber
for execution:



Solution: renewables and electric cars

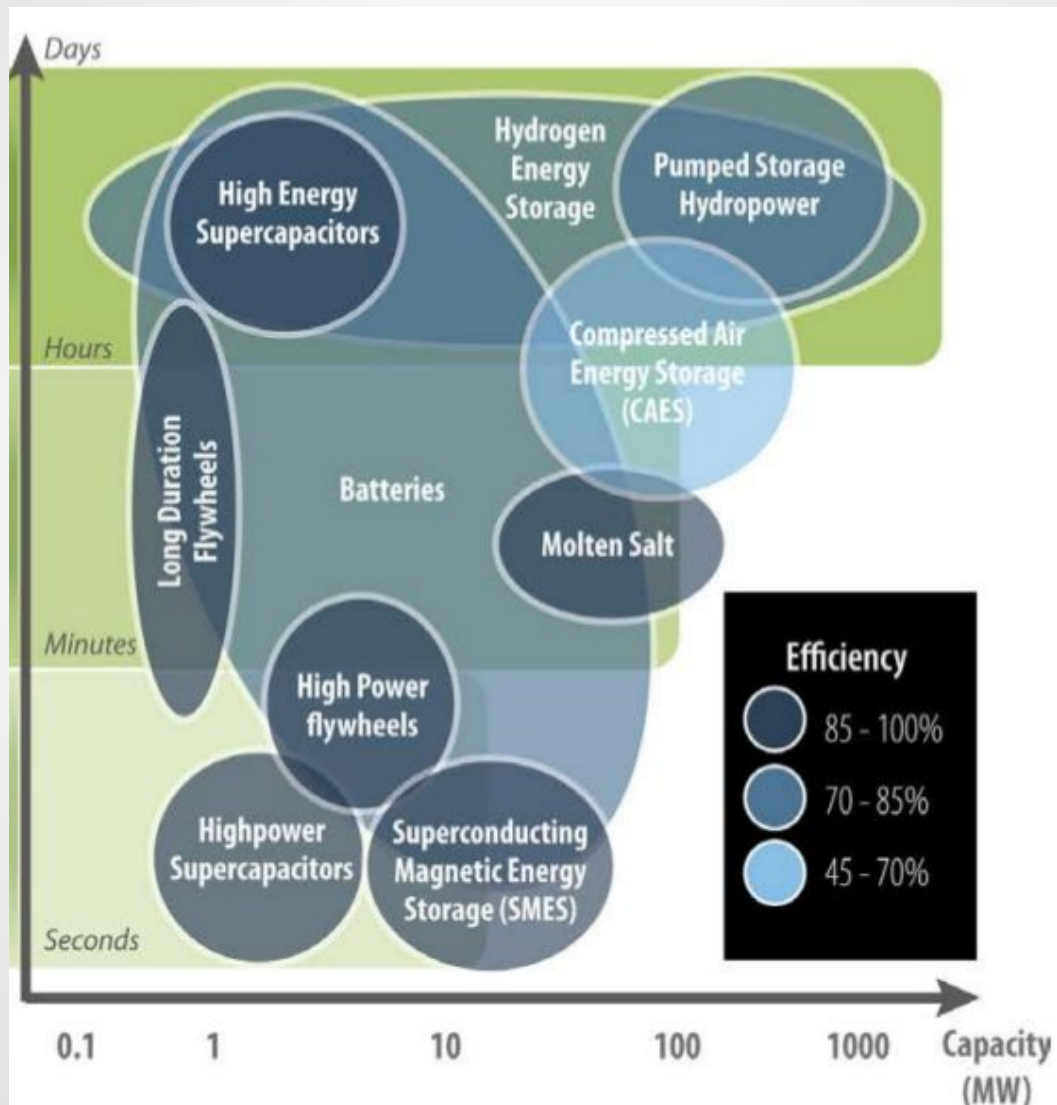
- Renewable electricity is unpredictable
- Electric cars - the range is limited - the price is high
- Both currently are economically unreasonable

What can change the situation?



Affordable energy storage!

Energy storage technologies



Among energy storage technologies **Li-ion** is the main for portable electronics, cars, and even grid storage

The best known advocate for Li-ion is Tesla



Model 3 up to
500 000 cars in 2020



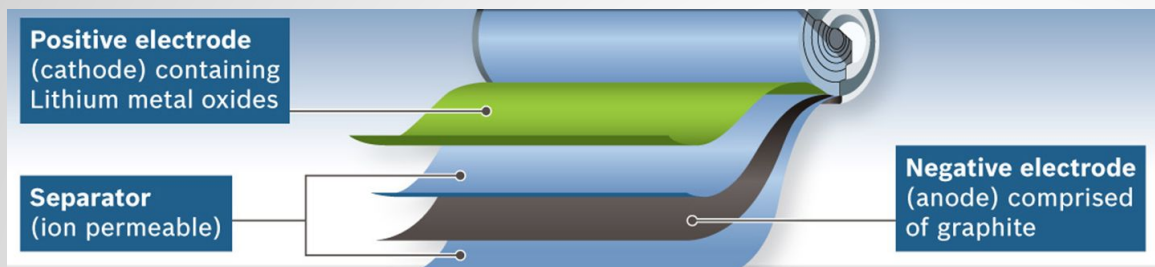
Tesla heavy Truck



Tesla Energy Solar + Li-ion

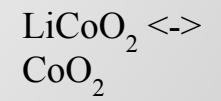
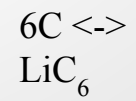
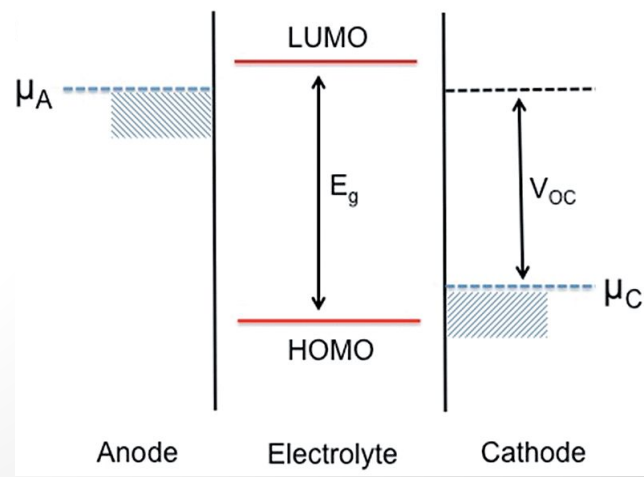
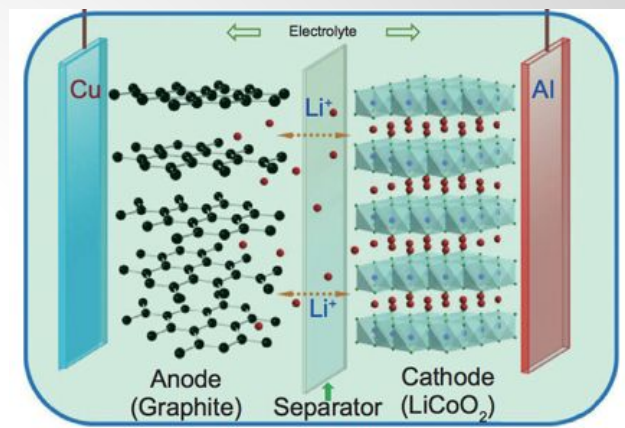
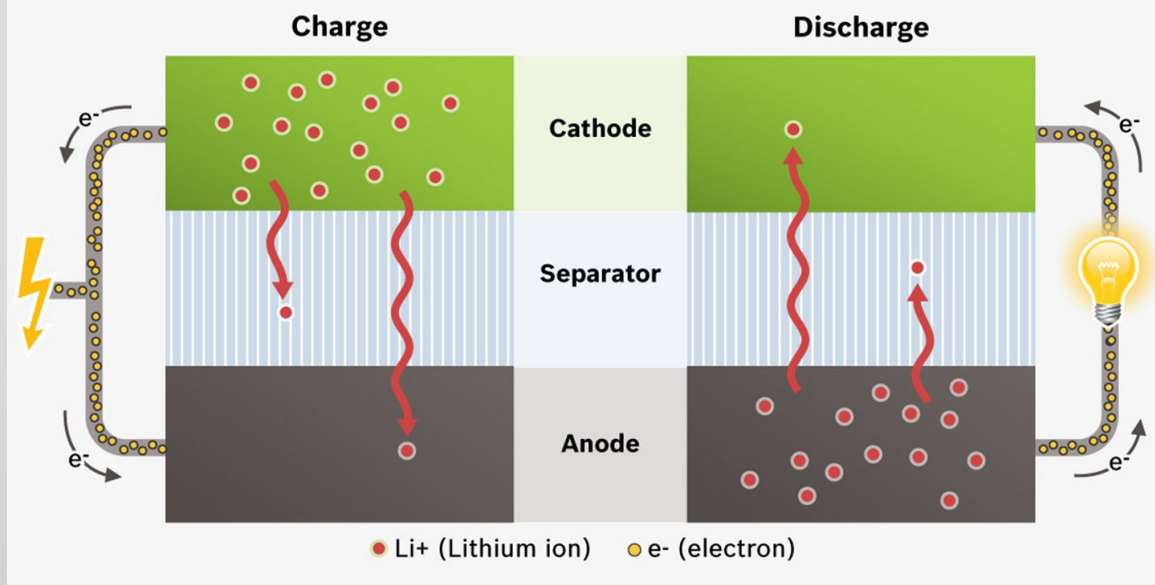


How the metal-ion battery works



➔ During **charge**, Lithium ions migrate towards the negative electrode. They store electrons from an external energy source.

➔ During **discharge**, Lithium loses electrons in the negative electrode. These electrons drive an external load.



Important battery metrics

Metric	Depends on
Voltage (V)	Chemistry and structure of cathode and anode, working window of electrolyte
Capacity (C)	Chemistry and structure of cathode and anode
Energy density	$E = \int V(C)dC$
Safety	Thermodynamical stability of cathode, anode, and electrolyte, battery construction
Power density	Ionic and electronic conductivity of cathode and anode

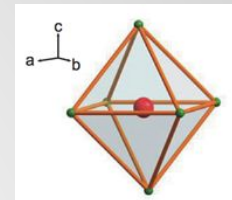
Both anode and cathodes are important! In our work we study cathodes

Main classes of cathode materials

CoO₆ octahedra

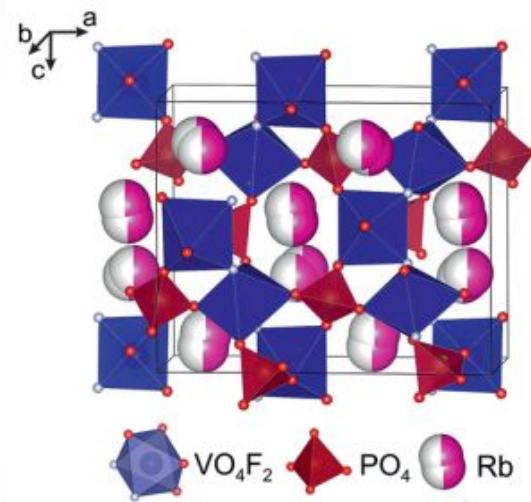
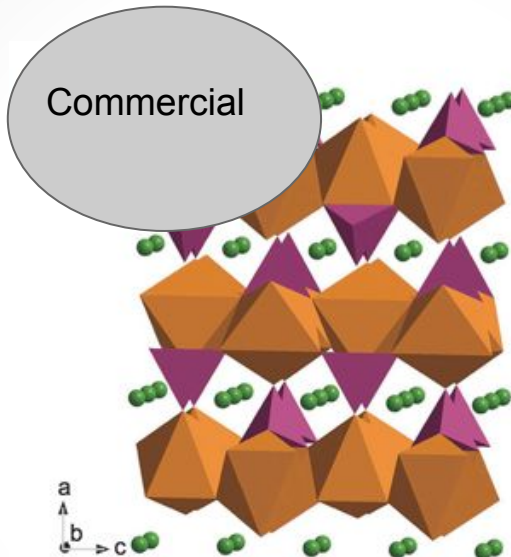
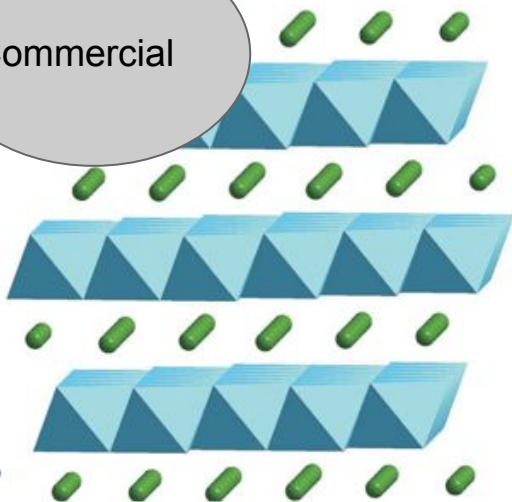
FeO₆ octahedra
PO₄ tetrahedra

VO₆ octahedra



Commercial

Commercial



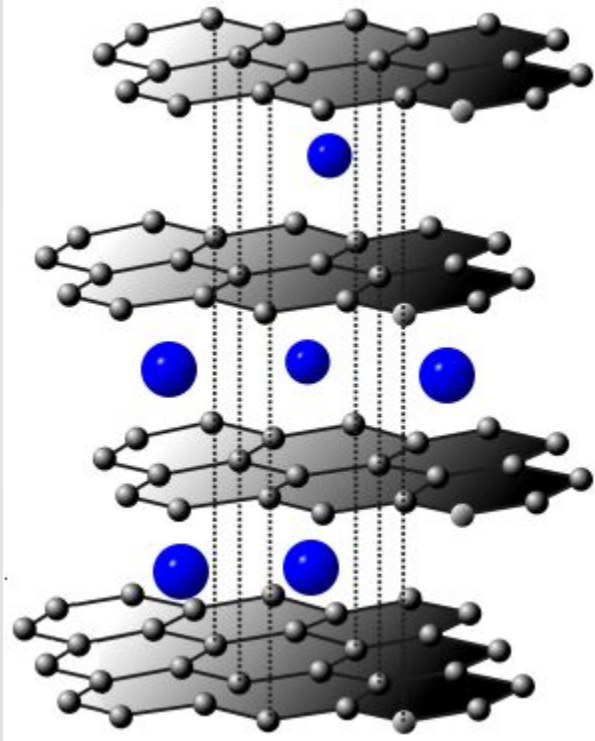
LiCoO₂, NaCoO₂
Layered oxides,
Transition metals are
Co, Mn, Ni
good for Li and Na

LiFePO₄, NaFePO₄
Olivines
High stability

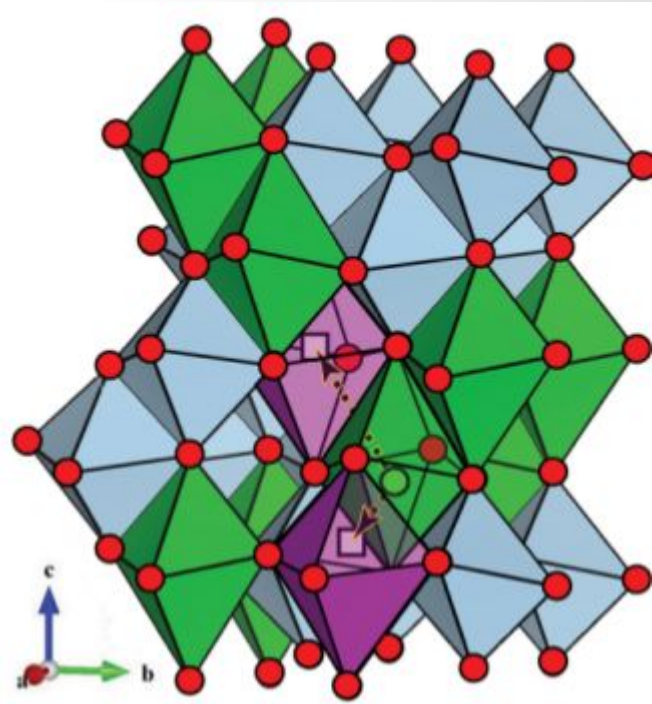
Other polyanion
materials, e.g.
KVPO₄F, Na₂FePO₄F,
etc. SO₄, SiO₄, BO₃
polyanion Li, Na and K

Anode materials

Graphite

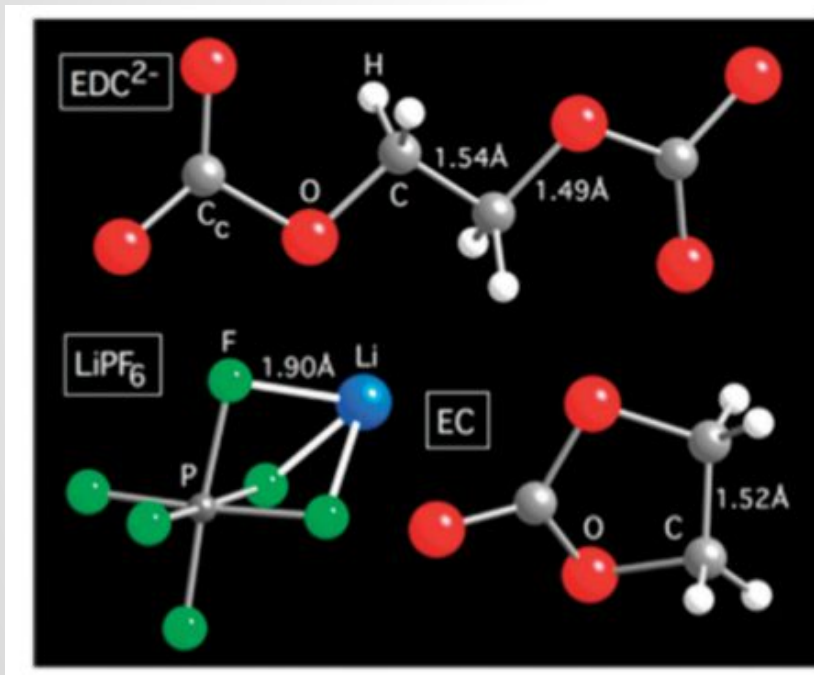


Anatase, LiTiO_2

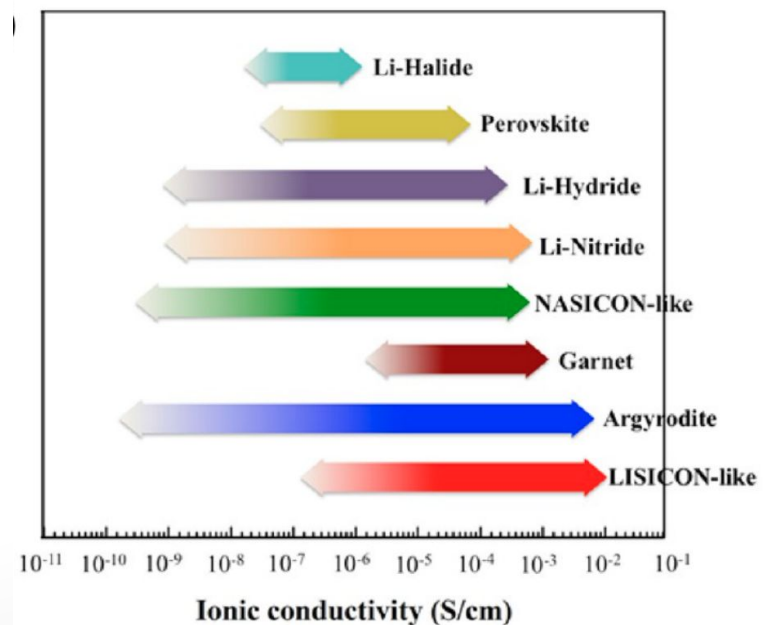


Electrolytes: liquid and solid

Li salts, such as LiPF_6 in organic solvents such as ethylene carbonate, propylene carbonate, etc



Solid electrolytes



Meesala, Yedukondalu, et al. "Recent advancements in Li-ion conductors for all-solid-state Li-ion batteries." *ACS Energy Letters* 2.12 (2017): 2734-2751.

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2. *Modeling of solid electrodes*
3. *Modeling of electrolytes and interfaces*
4. *High-throughput modeling*
5. *Few examples from our experience: OH defects in LiFePO_4 , antisite defects in layered oxides, migration barriers in cathodes*

Modeling of battery materials

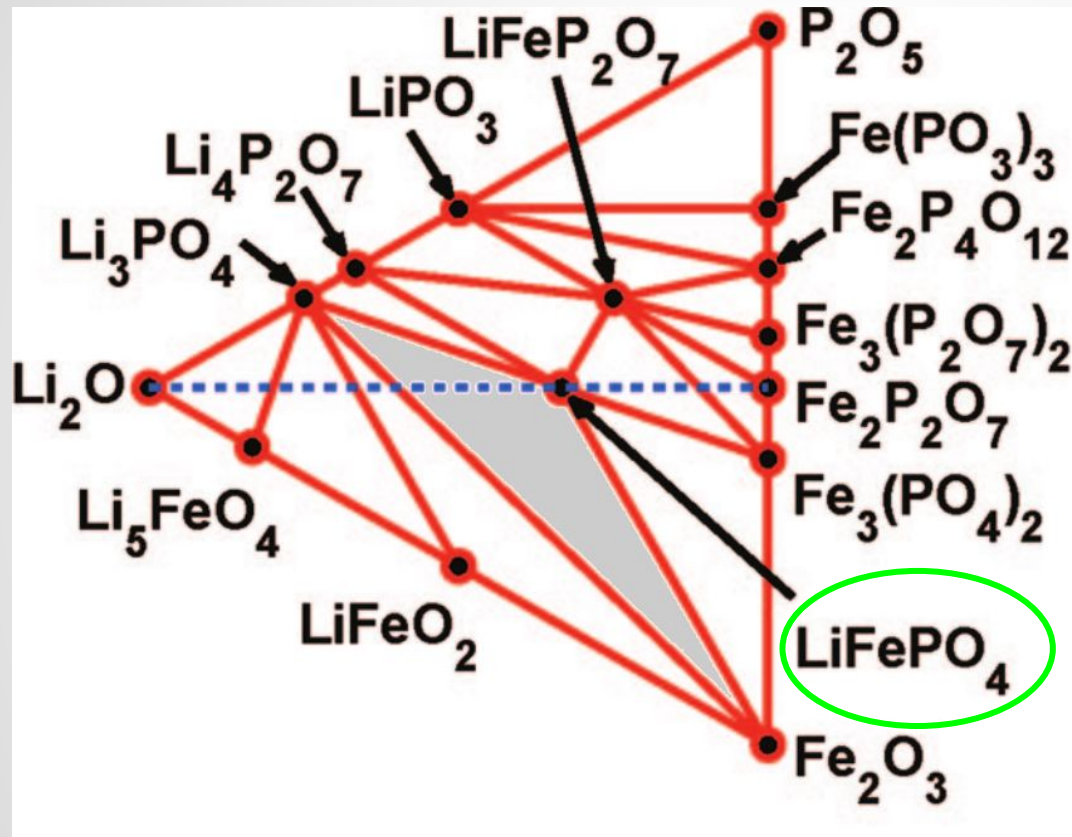
Cathodes, anodes, solid state conductors:

- Phase stability (DFT+U)
- Intercalation voltages and intercalation mechanism (DFT+U, Hybrid)
- Diffusivity of cations (DFT+U, MD)
- Defects and influence on properties(DFT+U)

Liquid electrolytes (DFT, MD):

- Solvation energies (MP2, CI, CC, DFT)
- Electrolyte stability (MP2, CI, CC, DFT)

Li-Fe-P-O phase diagram, $\mu(\text{O}_2) = -12.4 \text{ eV}$



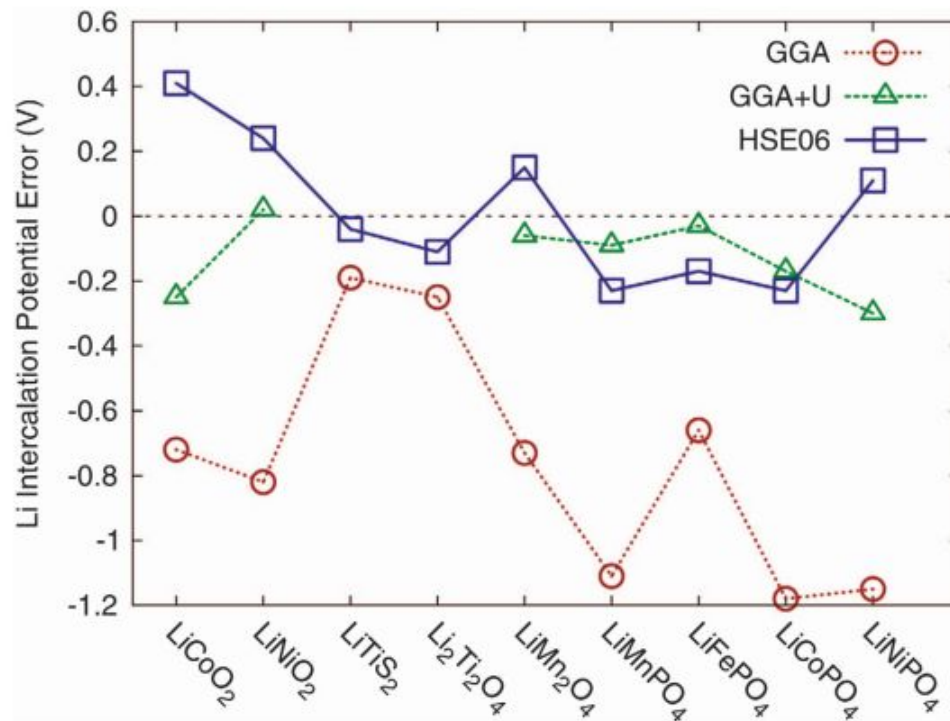
$$\bar{\varphi}(\mu_{\text{O}_2}, x_{\text{Li}}, x_{\text{Fe}}, x_{\text{P}}) \approx \frac{E - \mu_{\text{O}_2} N_{\text{O}_2}}{N_{\text{Li}} + N_{\text{Fe}} + N_{\text{P}}}$$

1. Ong, S.P., Wang, L., Kang, B. and Ceder, G. Li-Fe-P-O₂ Phase Diagram from First Principles Calculations. Chemistry of Materials. 20, 5 (Mar. 2008), 1798–1807.

Average intercalation voltage

$$\bar{V}(x_1, x_2) \approx -\frac{E(\text{Li}_{x_1}\text{MO}_2) - E(\text{Li}_{x_2}\text{MO}_2) - (x_1 - x_2) E(\text{Li})}{(x_1 - x_2) F}$$

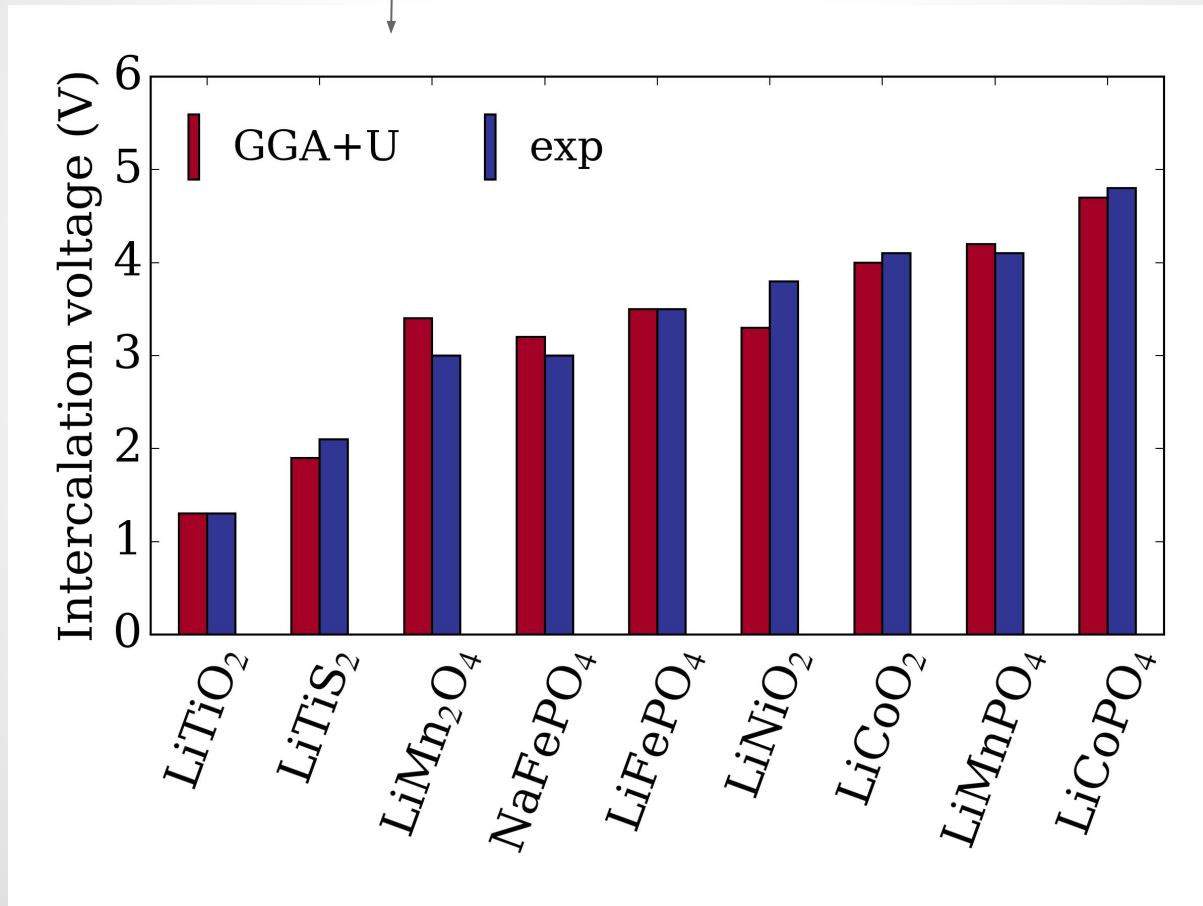
with $x_1 > x_2$,



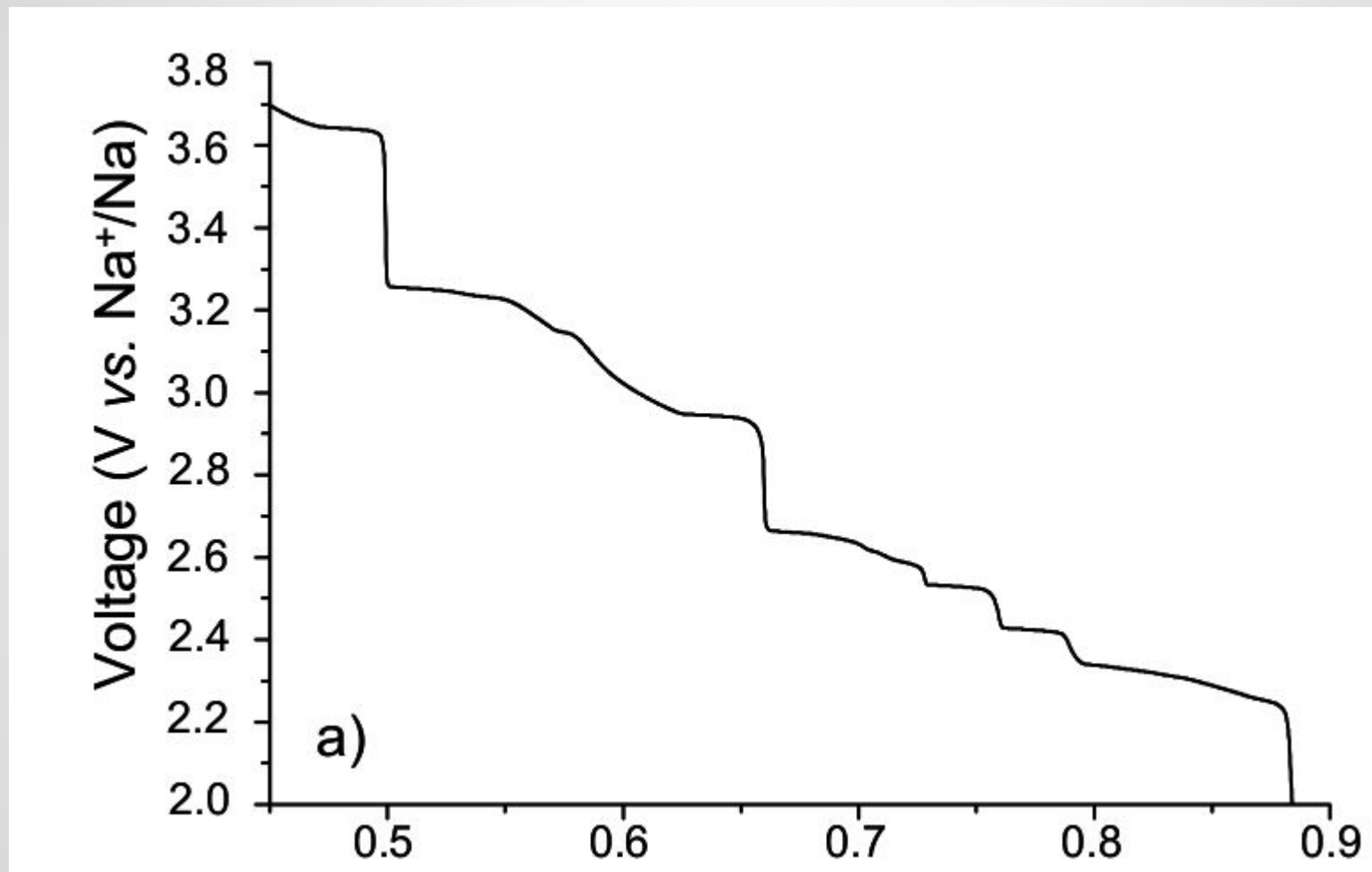
Urban, A. et al. // *npj Computational Materials* 2.1 (2016): 1-13.

DFT+U calculations

$x_1 = 100 \%$, $x_2 = 0 \%$



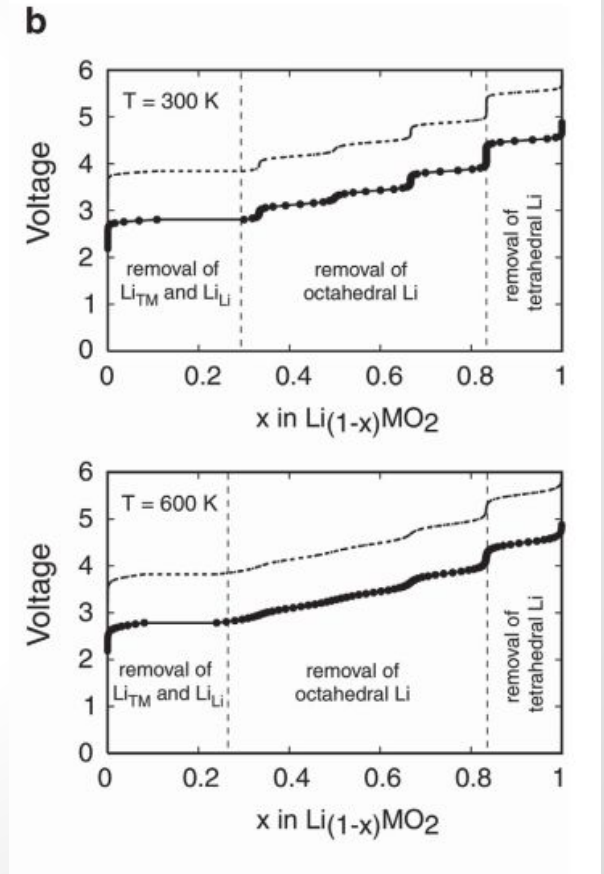
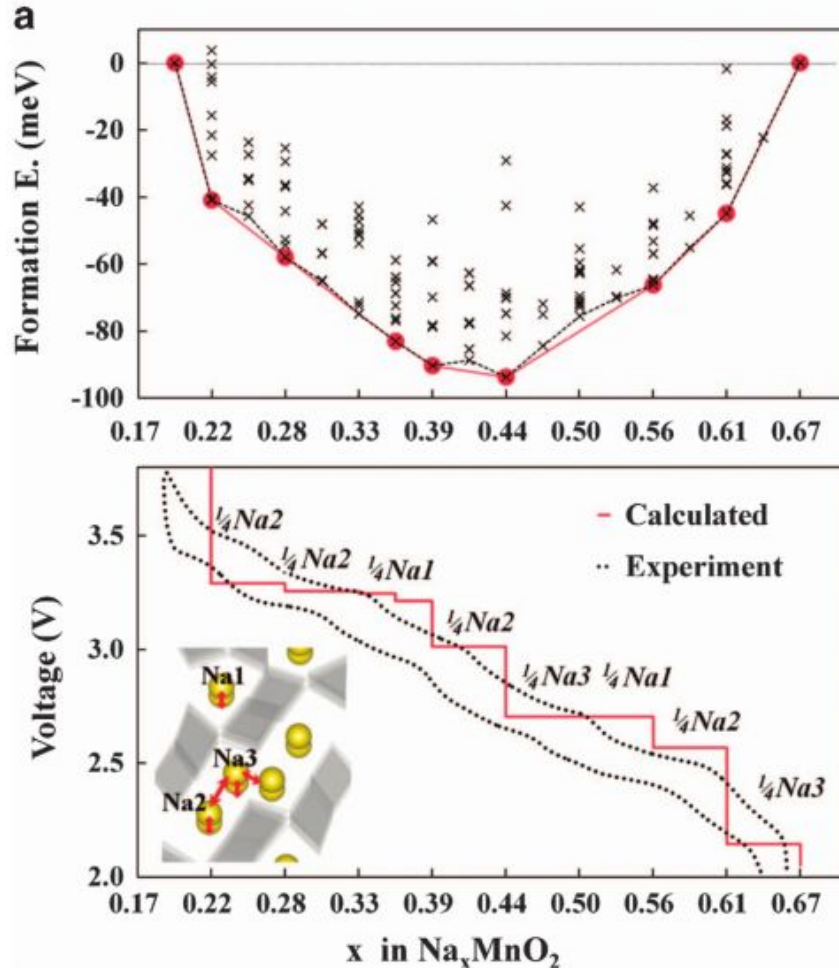
Voltage profile NaCoO₂ (P2)



berthelot2011_SI_nature

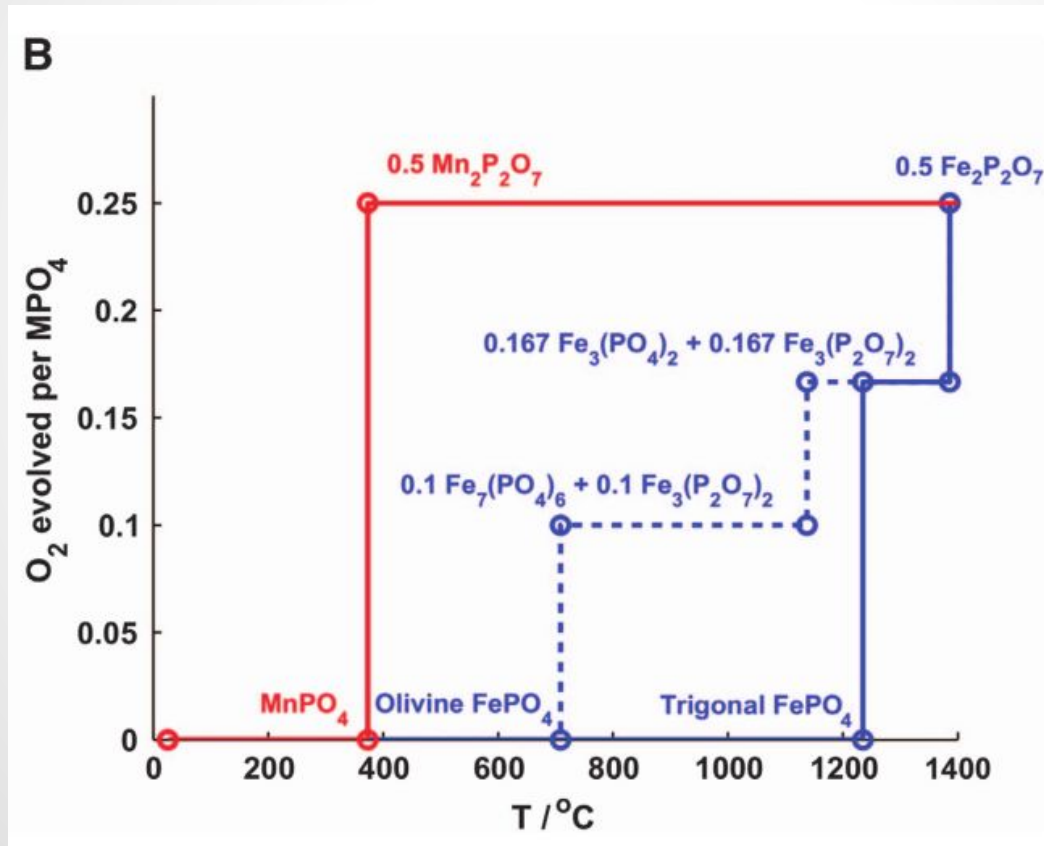
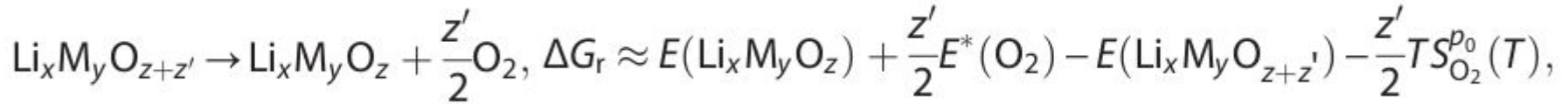
Calculation of voltage profiles

$$E_f(\text{Li}_x\text{MO}_2) = E(\text{Li}_x\text{MO}_2) - x E(\text{LiMO}_2) - (1-x) E(\text{MO}_2),$$



Urban, A. et al.// *npj Computational Materials* 2.1 (2016): 1-13.

Thermal stability of electrode



Urban, A. et al. // *npj Computational Materials* 2.1 (2016): 1-13.

Main errors in DFT+U for calculating formation energies of cathode materials

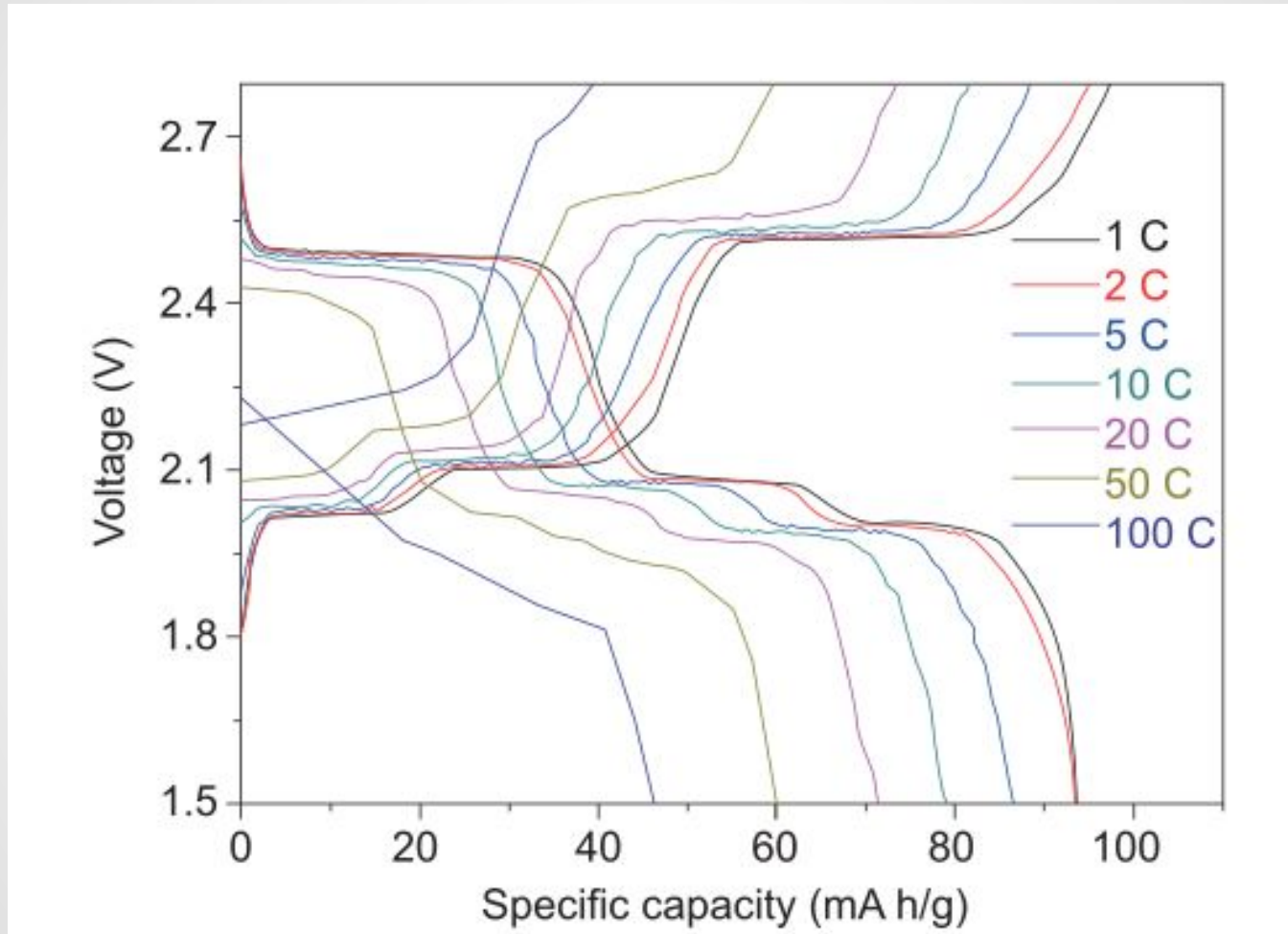
(i) a constant energy shift of the DFT O_2 energy to account for overbinding fixed by constant correction

(ii) a Hubbard U correction

using U values fitted to experimental oxide formation energies error in the formation energies of transition-metal oxides from up to 1.0 eV with GGA to less than 0.1 eV in most cases.

Urban, A. et al. // *npj Computational Materials* 2.1 (2016): 1-13.

Typical galvanostatic curve at different C-rates shows diffusion limitation

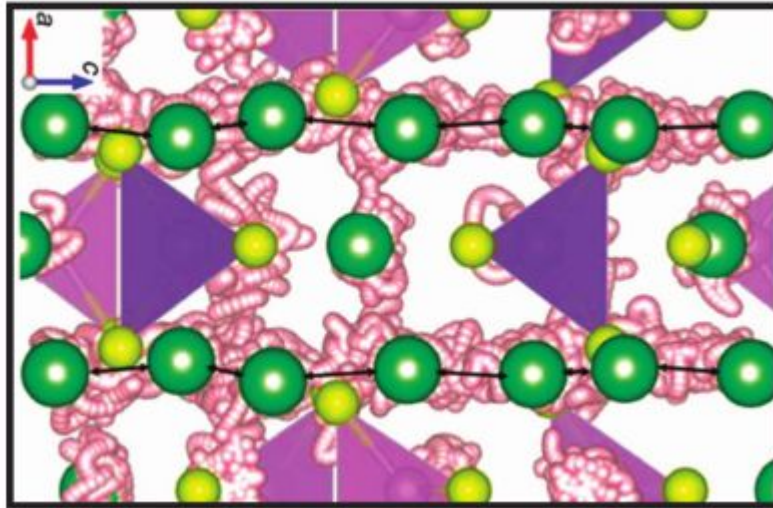


LVP//LTO battery

Massé, Robert C., et al. "Energy storage through intercalation reactions: electrodes for rechargeable batteries." *National Science Review* 4.1 (2017): 26-53.

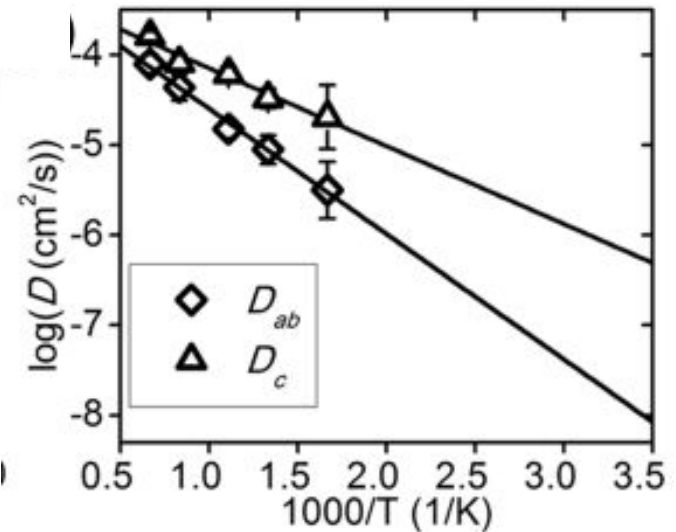
Ionic conductivity, Ab initio MD

Li trajectories in $\text{Li}_{10}\text{GeP}_2\text{S}_{12}$ at 900 K



$$\sigma(T) = \frac{N_{\text{Li}} e^2}{V k_B T} D(T),$$

Nernst–Einstein relation for ionic conductivity. N_{Li} is the number of lithium ions, V is the volume of the simulation cell



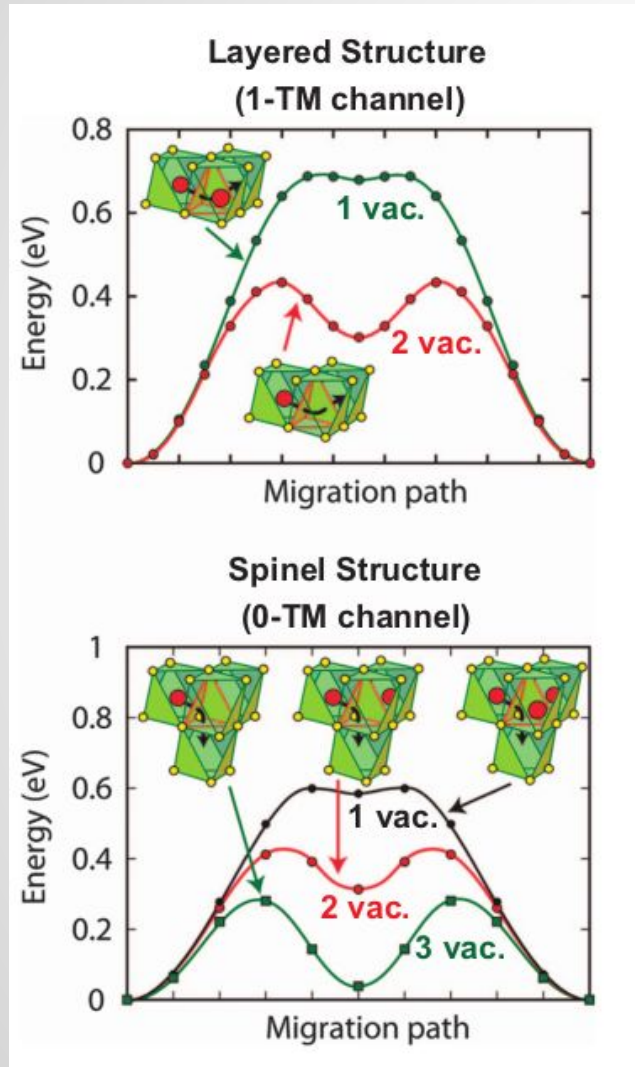
$$D(T) \approx D_0 e^{-\frac{E_a}{k_B T}},$$

Arrhenius law: E_a is activation energy for diffusion

Urban, A. et al.// *npj Computational Materials* 2.1 (2016): 1-13.

Mo, Yifei, Shyue Ping Ong, and Gerbrand Ceder. " *Chemistry of Materials* 24.1 (2012): 15-17.

Diffusivity based on 0 K migration barriers



Rate of the hopping process

$$k(T) = \nu^*(T) e^{-\frac{\Delta G^\ddagger(T)}{k_B T}},$$

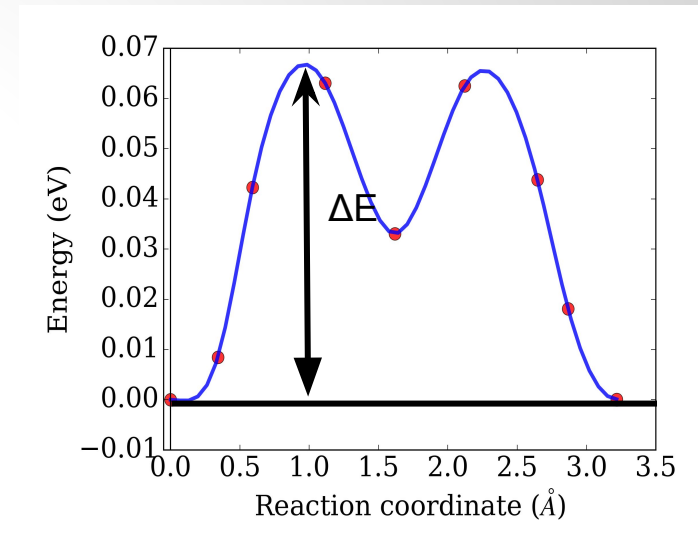
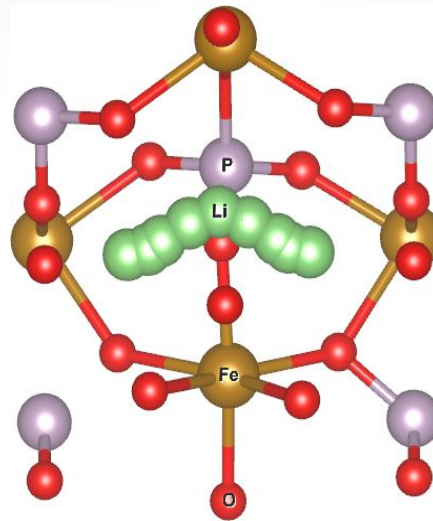
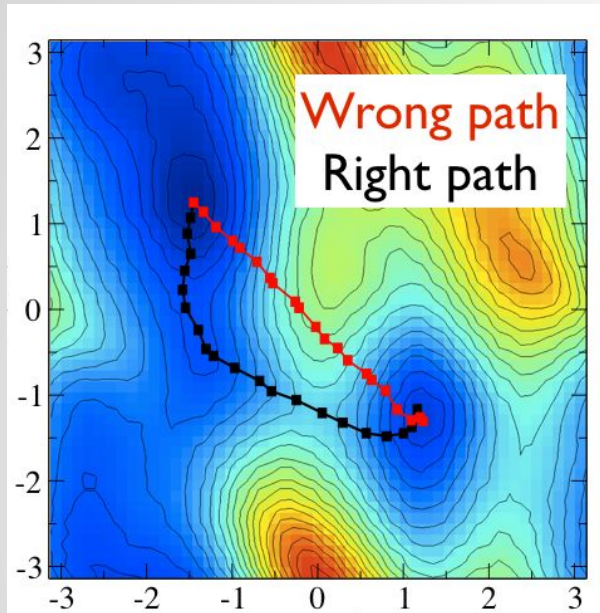
ν^* is temperature-dependent effective attempt frequency, ΔG^\ddagger is Gibbs free energy of activation (migration barrier)

$$D \approx g \cdot a^2 \cdot k,$$

a is hopping distance, g is geometrical factor (~ 1)

Typical values for the prefactor ν^* are 10^{11} to 10^{13} s^{-1}

NEB method for finding saddle points



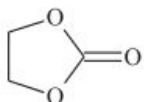
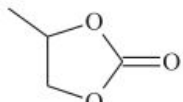
Nudged elastic band method (NEB) is used to find minimum energy paths and migration barriers at saddle points.

The spring forces keep the images spaces equally, allowing to propagate a chain towards minimum energy path.

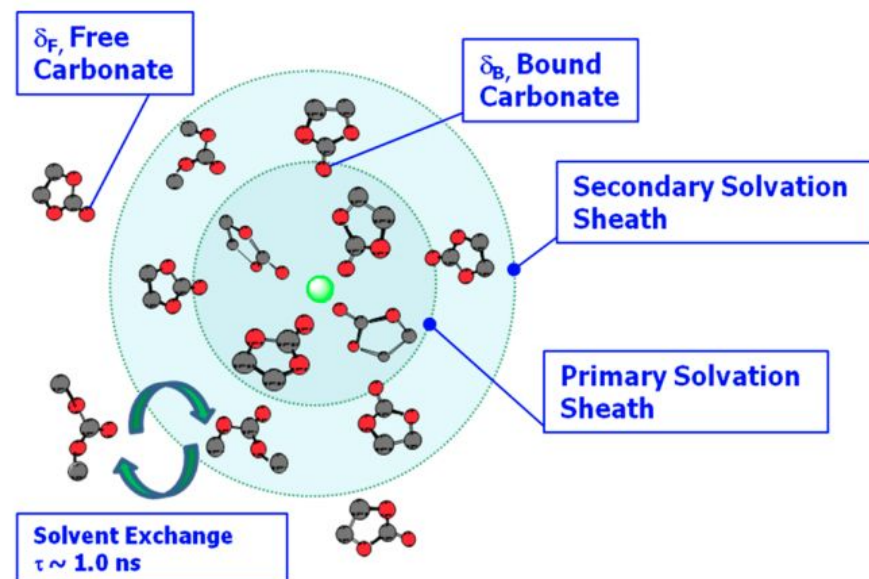
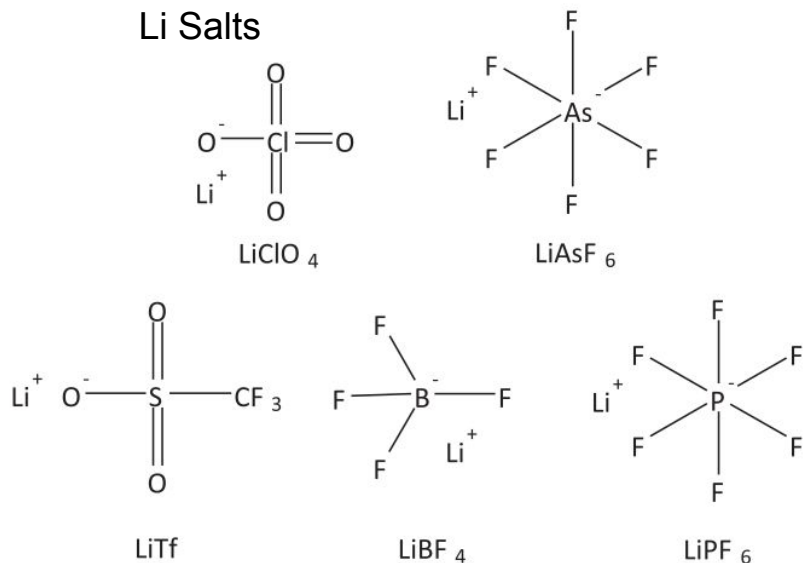
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- 2. Modeling of solid electrodes*
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Modeling of electrolyte

Solvent	Structure	M. Wt	$T_m/^\circ\text{C}$	$T_b/^\circ\text{C}$	η/cP 25 °C	ϵ 25 °C
EC		88	36.4	248	1.90 (40 °C)	89.78
PC		102	-48.8	242	2.53	64.92

Li Salts

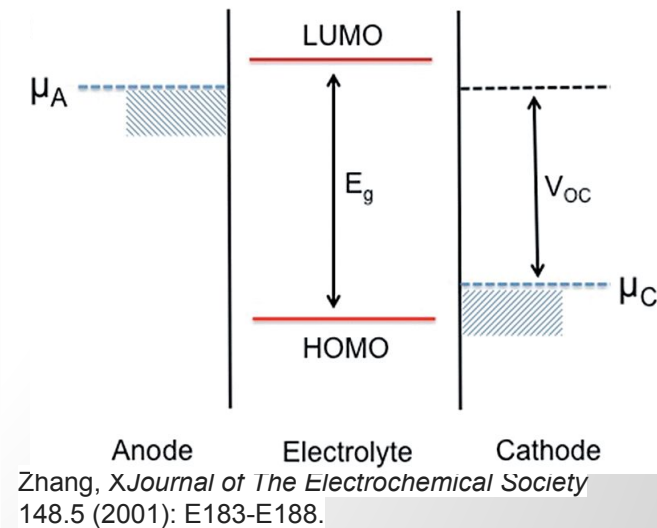
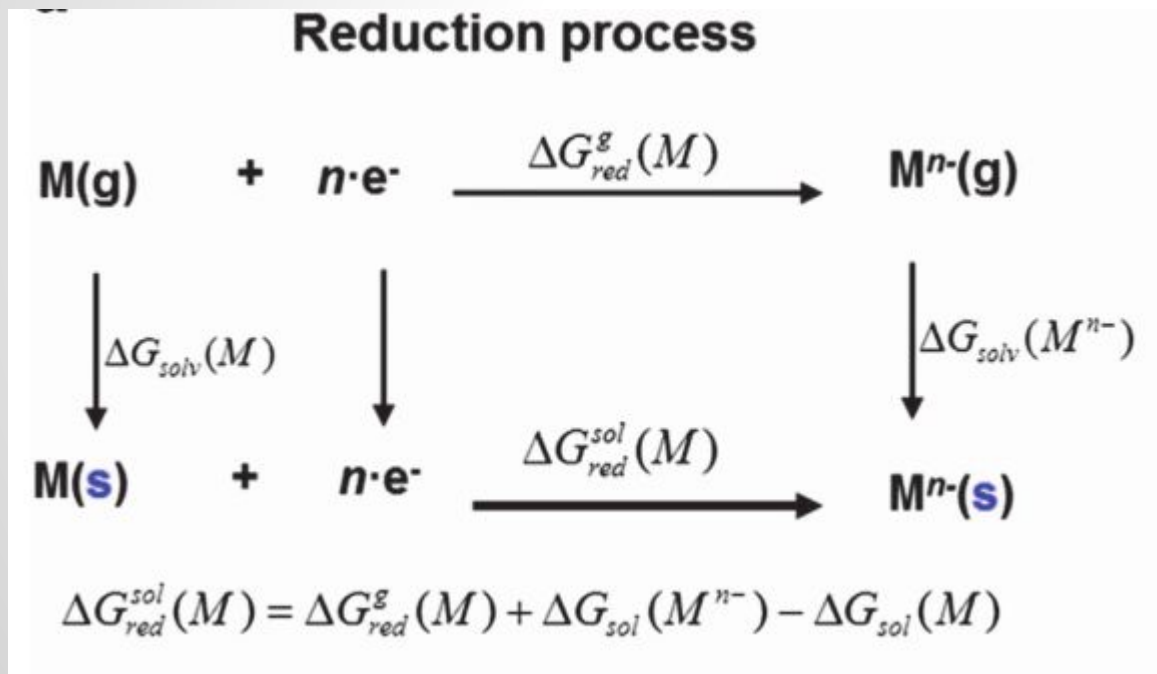


Marcinek, M., et al. *Solid State Ionics* 276 (2015): 107-126.

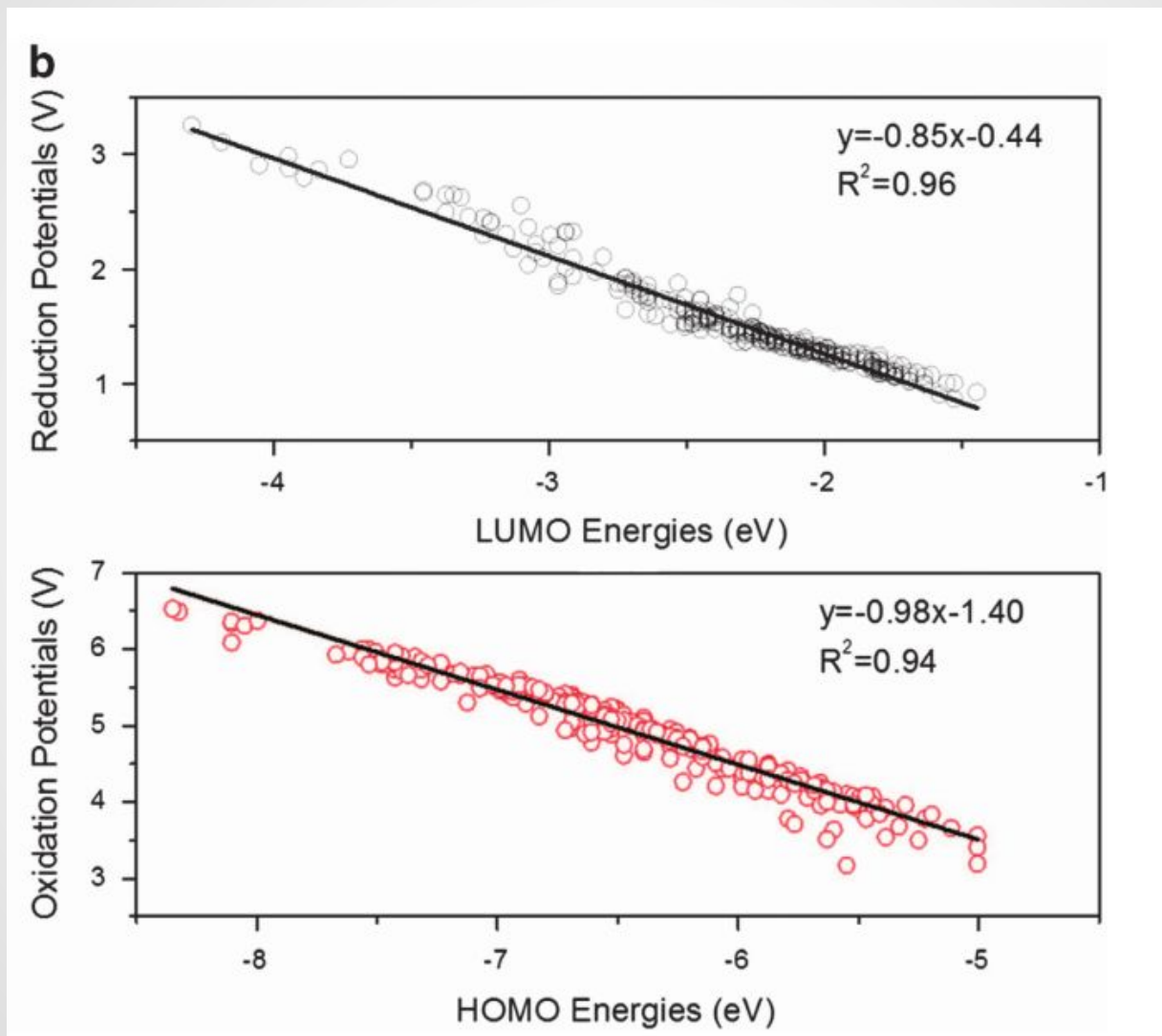
Bogle, X, et al. *The journal of physical chemistry letters* 4.10 (2013): 1664-1668.

Electrochemical stability of electrolytes

reduction : $\Delta G_{\text{red}}^{\text{S}} = G[\text{M}^{n-}(\text{s})] - G[\text{M}(\text{s})] - nG[\text{e}^{-}(\text{s})]$
 oxidation : $\Delta G_{\text{ox}}^{\text{S}} = G[\text{M}^{n+}(\text{s})] + nG[\text{e}^{-}(\text{s})] - G[\text{M}(\text{s})],$



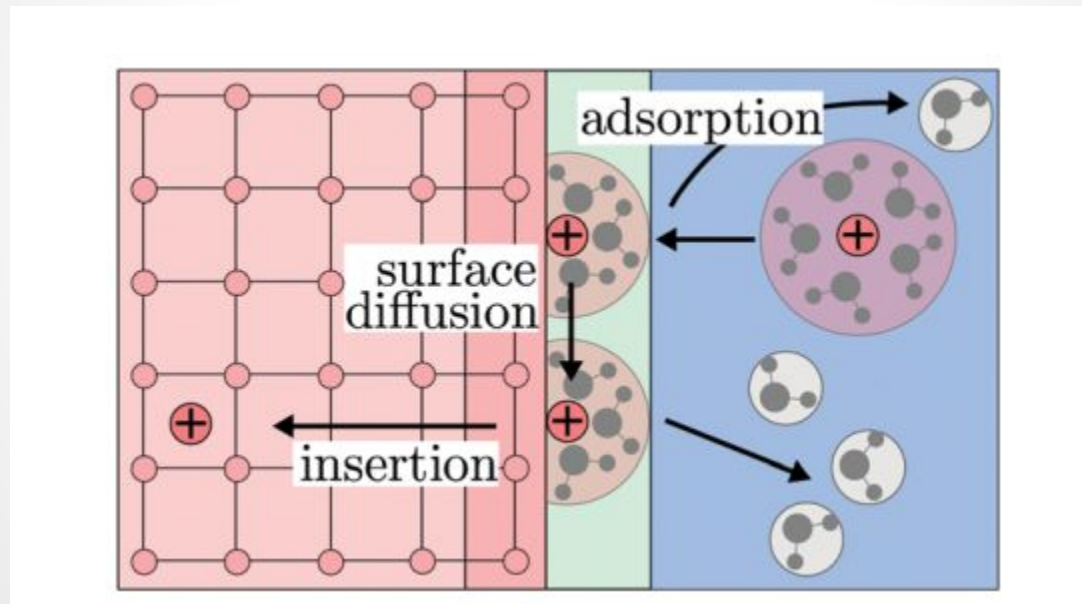
HOMO and LUMO for screening electrolytes



Cheng, L, et al. " *The journal of physical chemistry letters* 6.2 (2015): 283-291.

Electrolyte/electrode interface the largest challenge for modelling now

Diffusion is only half of the story, kinetics of interphase charge transfer is highly important



Li, Yunsong, and Yue Qi. "Energy landscape of the charge transfer reaction at the complex Li/SEI/electrolyte interface." *Energy & Environmental Science* 12.4 (2019): 1286-1295.

Lück, Jessica, and Arnulf Latz. "Modeling of the electrochemical double layer and its impact on intercalation reactions." *Physical Chemistry Chemical Physics* 20.44 (2018): 27804-27821.

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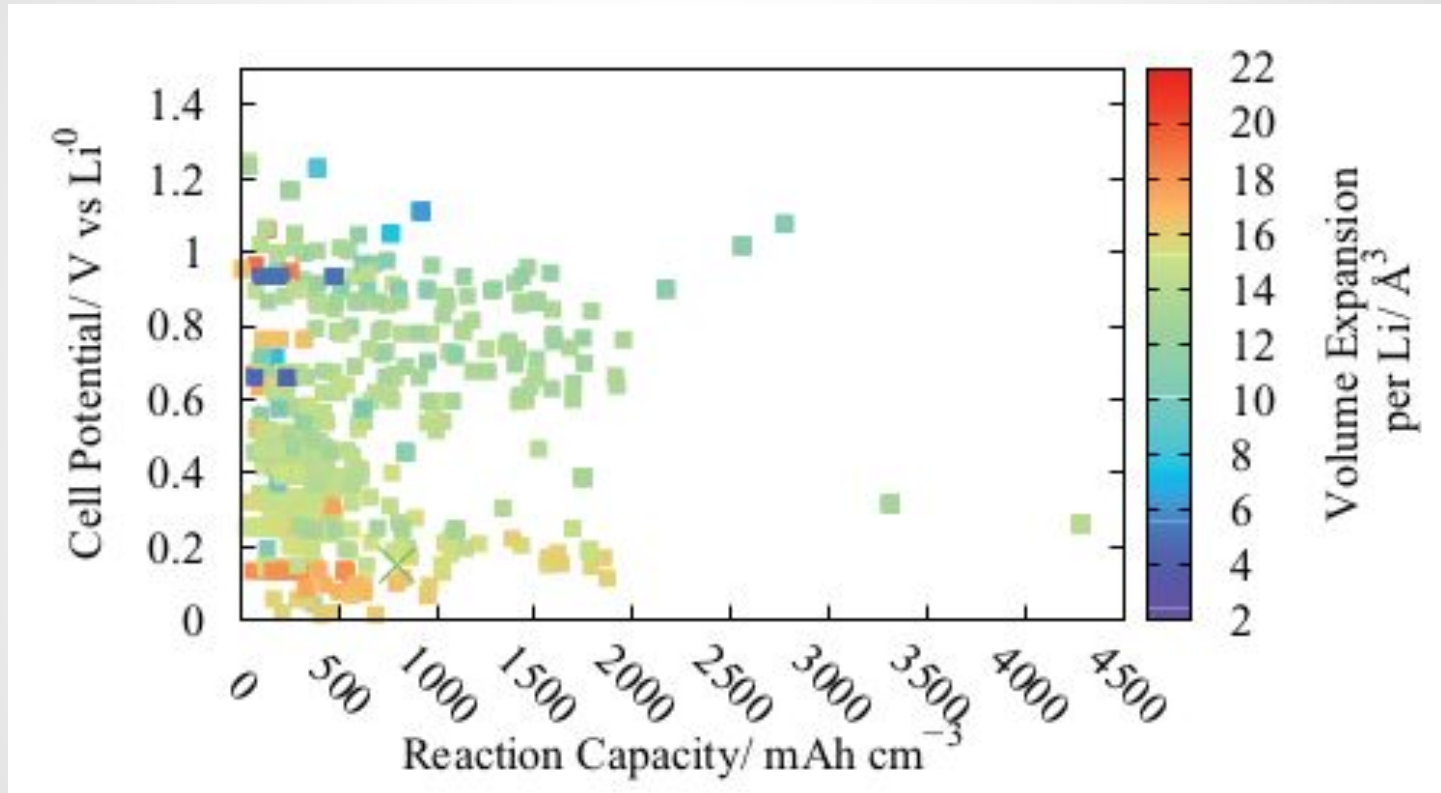
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What is high-throughput (HT) computational materials design?

- the amount of data is way too high to be produced or analyzed by direct intervention of researcher - therefore must be performed automatically
- the results are stored in database, which is further analyzed for selecting novel materials or gaining new physical insights

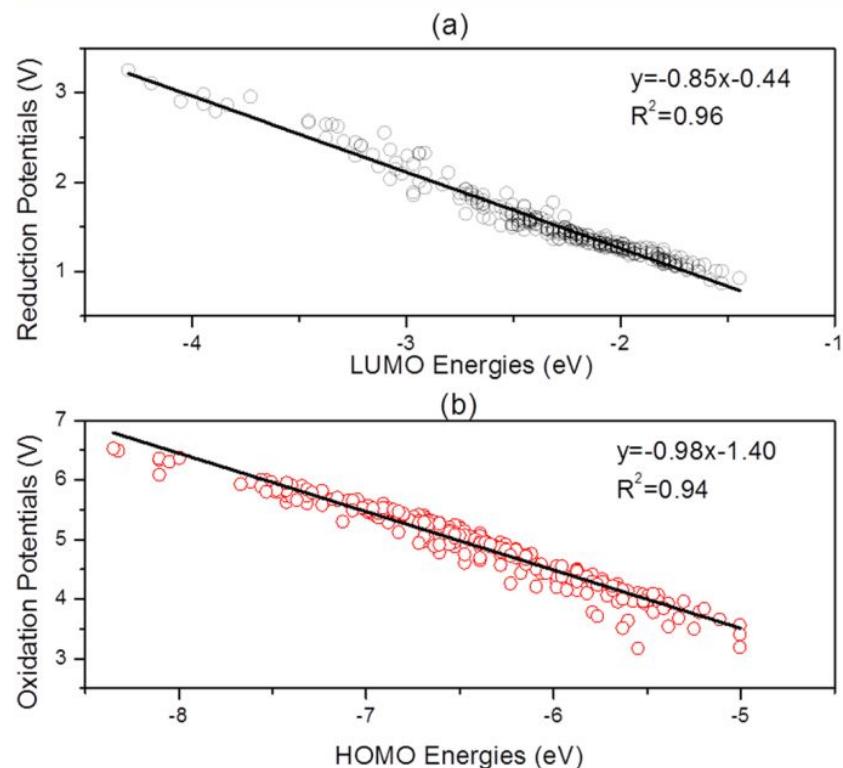
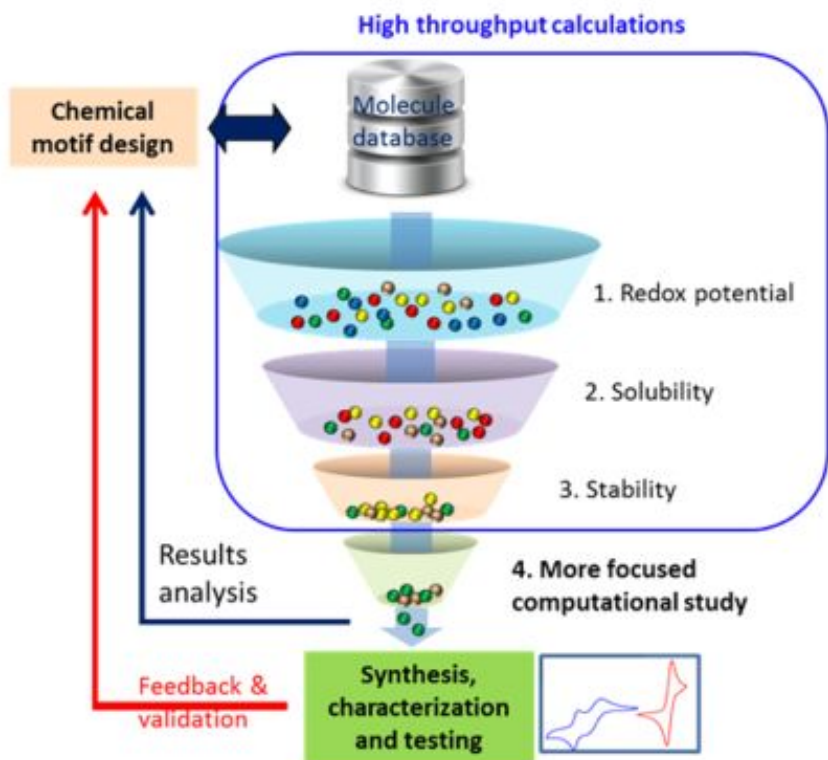
The next step and a revolution in computational materials design!

High-throughput computational screening of new Li-ion battery anode materials



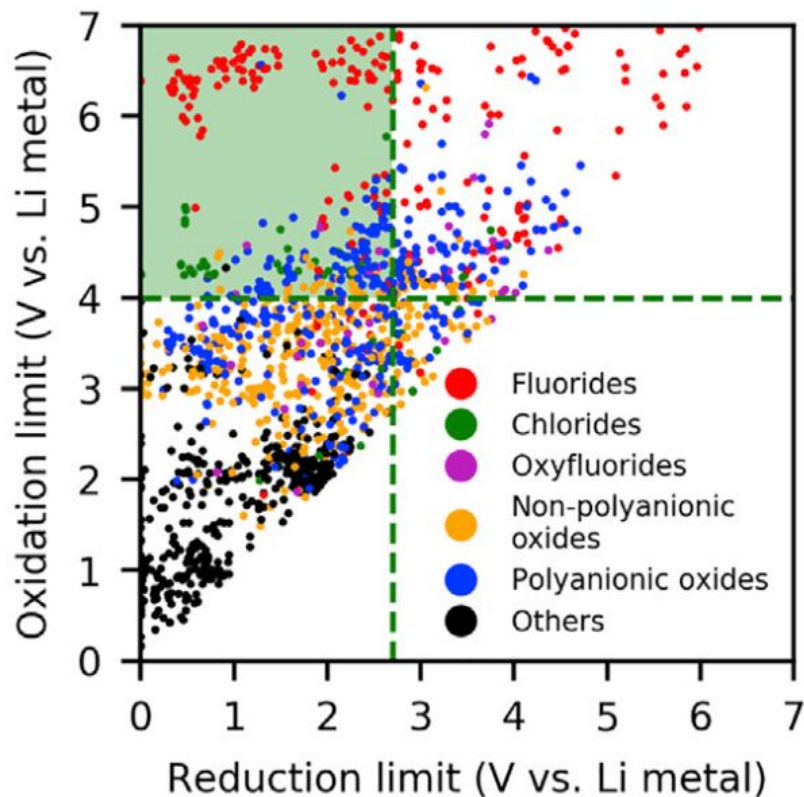
Kirklin, Scott, Bryce Meredig, and Chris Wolverton. "High-throughput computational screening of new Li-ion battery anode materials." *Advanced Energy Materials* 3.2 (2013): 252-262.

High-throughput Electrolyte discovery



Cheng, Lei, et al. "Accelerating electrolyte discovery for energy storage with high-throughput screening." *The journal of physical chemistry letters* 6.2 (2015): 283-291.

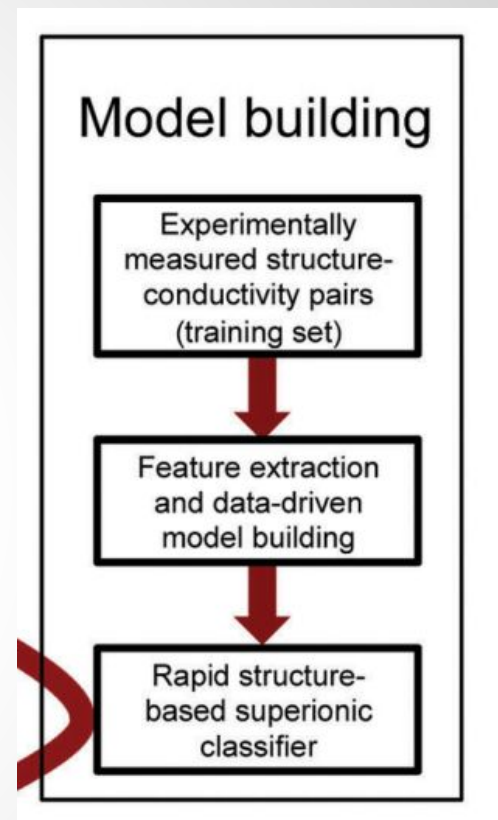
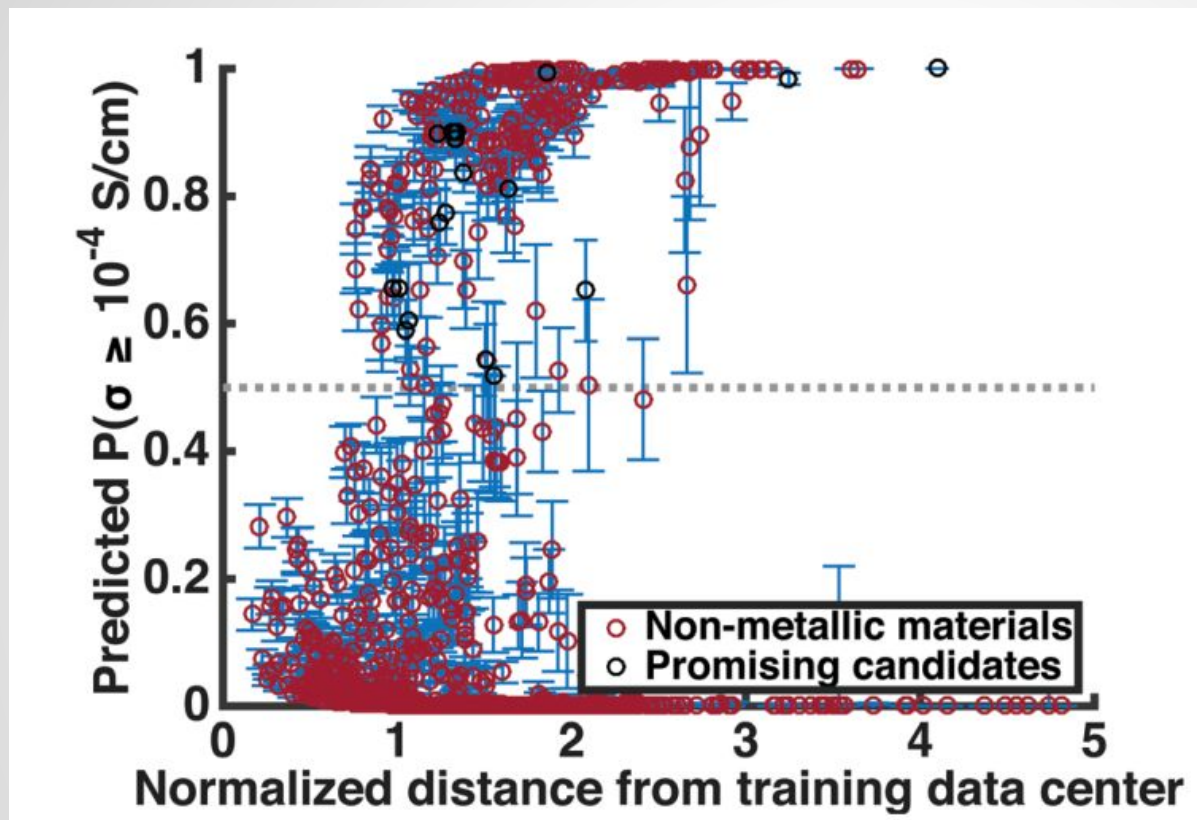
Screening of Cathode Coatings for Solid-State Batteries



Coatings	ICSD #	Calculated Migration Barrier (eV)	Experimental Activation Energy (eV)
Li_2ZrO_3	31941	0.48	0.5, ⁷⁷ 0.68 ⁷⁸
LiH_2PO_4	100200	0.33	— ^a
$\text{LiTi}_2(\text{PO}_4)_3$	95979	0.42	0.47 ⁷⁹
$\text{LiBa}(\text{B}_3\text{O}_5)_3$	93013	1.96	—
LiPO_3	51630	0.40	1.40 ⁸²
$\text{LiLa}(\text{PO}_3)_4$	416877	1.39	0.92 ^{b81}
$\text{LiCs}(\text{PO}_3)_2$	62514	1.27	1.31 ⁸⁰

Xiao, Yihan, et al. "Computational screening of cathode coatings for solid-state batteries." *Joule* 3.5 (2019): 1252-1275.

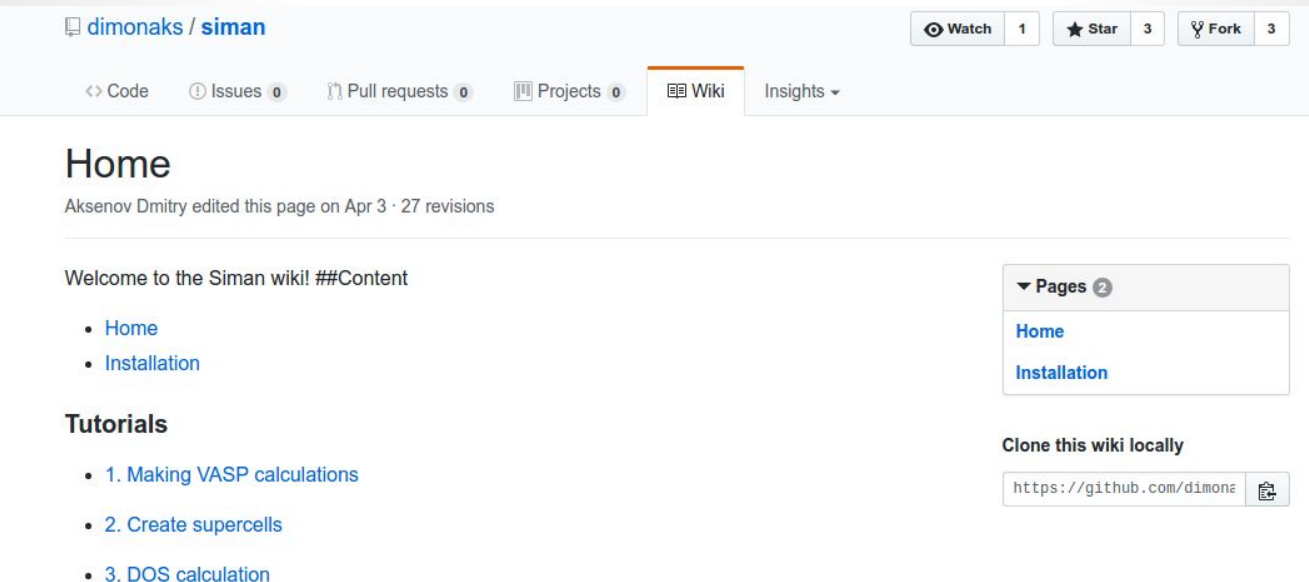
Screening of more than 12 000 candidates for solid lithium-ion conductor materials



Sendek, Austin D., et al. "Holistic computational structure screening of more than 12000 candidates for solid lithium-ion conductor materials." *Energy & Environmental Science* 10.1 (2017): 306-320.

Development of code SIMAN for Automation of DFT calculations

- **SIMAN** package, on github <https://github.com/dimonaks/siman> (~30 000 lines of code)
 - generation of input files for VASP (DFT) or other codes
 - batch submission of hundreds of jobs and workflows
 - extraction and advanced analysis of output results

○ 

Optimize volume using Siman at two e-cut

```
1 new = InputSet()  
2 new.read_incar('INCAR')
```

The set can be added to the predefined persistent dictionary by

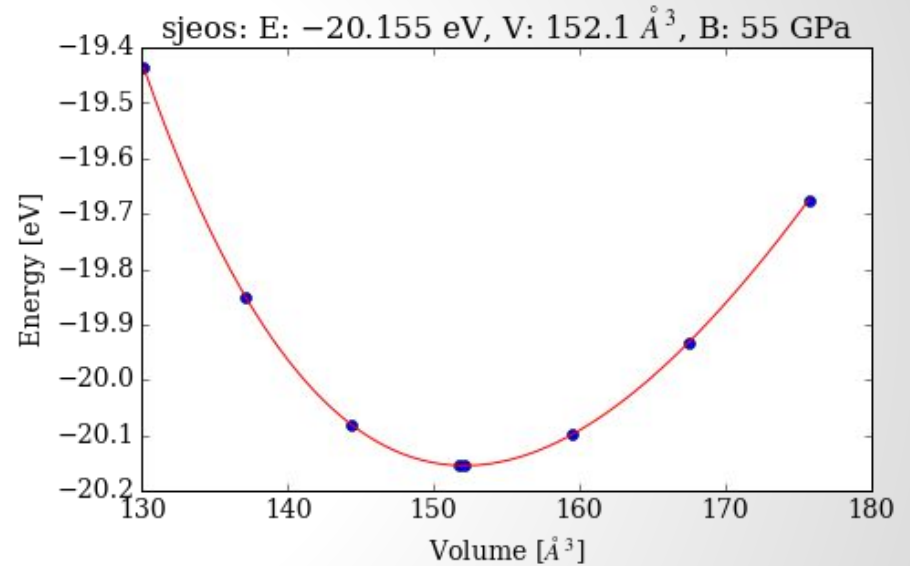
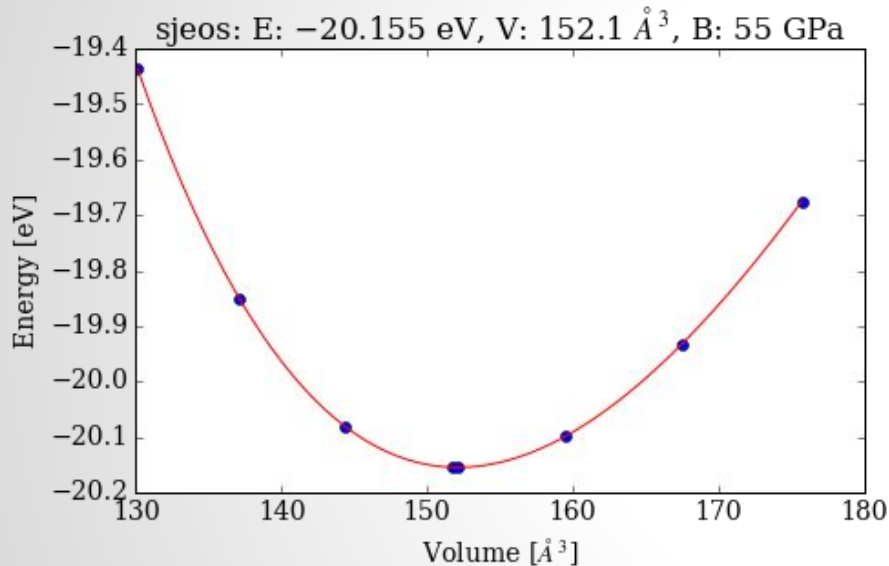
```
1 sets['S400'] = new
```

```
1 read_vasp_sets([( 'S600', 'S400', { 'ENCUT': 600 } )])
```

```
1 add('Li2bcc', ['S400', 'S600'], 1, run = 1,  
      calc_method = 'uniform_scale')
```

Results of optimization

```
1 res('Li2bcc', ['S400', 'S600'],  
      [1,2,3,4,5,6,7,100], analys_type = 'fit_a')
```



- In the same manner, each step required in calculations is automated
- Very useful when you have several structures and elements to study

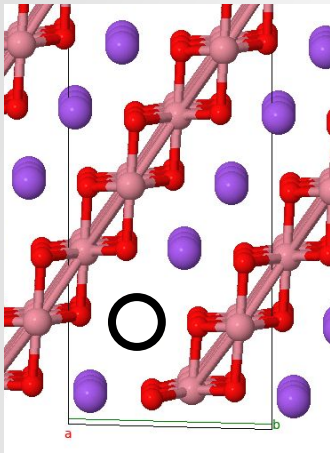
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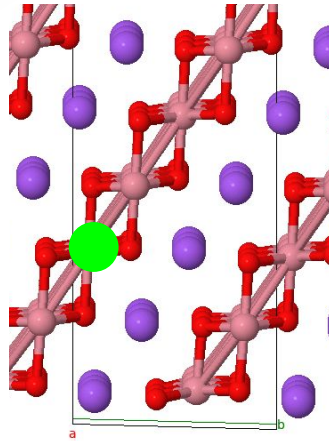
Our method for electronic structure calculation

- DFT + U (VASP code)
- $U = 6.2$ (Ni), 3.4 (Co) , 4.0 (Fe), 3.1 (V) eV
- PAW PBE potentials
- Spin polarized ferromagnetic
- Dipole correction for slab
- Energy cut-off 400 eV
- kpoint density 0.03 \AA^{-1}
- Forces less than 0.05 eV/\AA

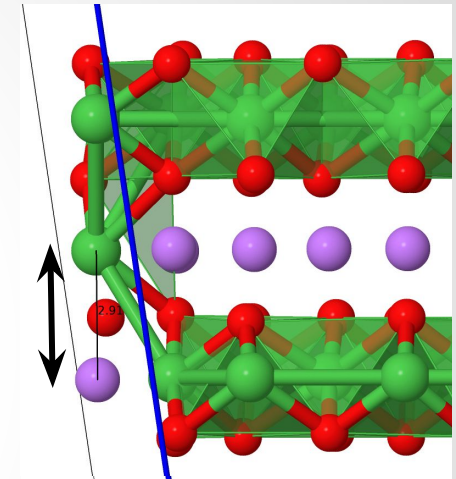
Case study: point defects in cathodes



Vacancies



Dopants

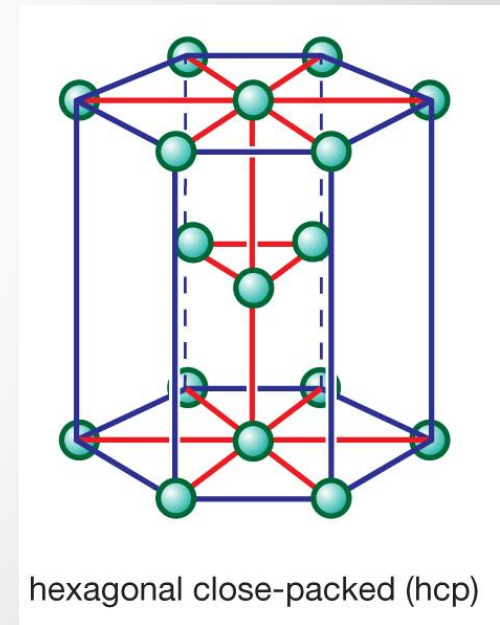
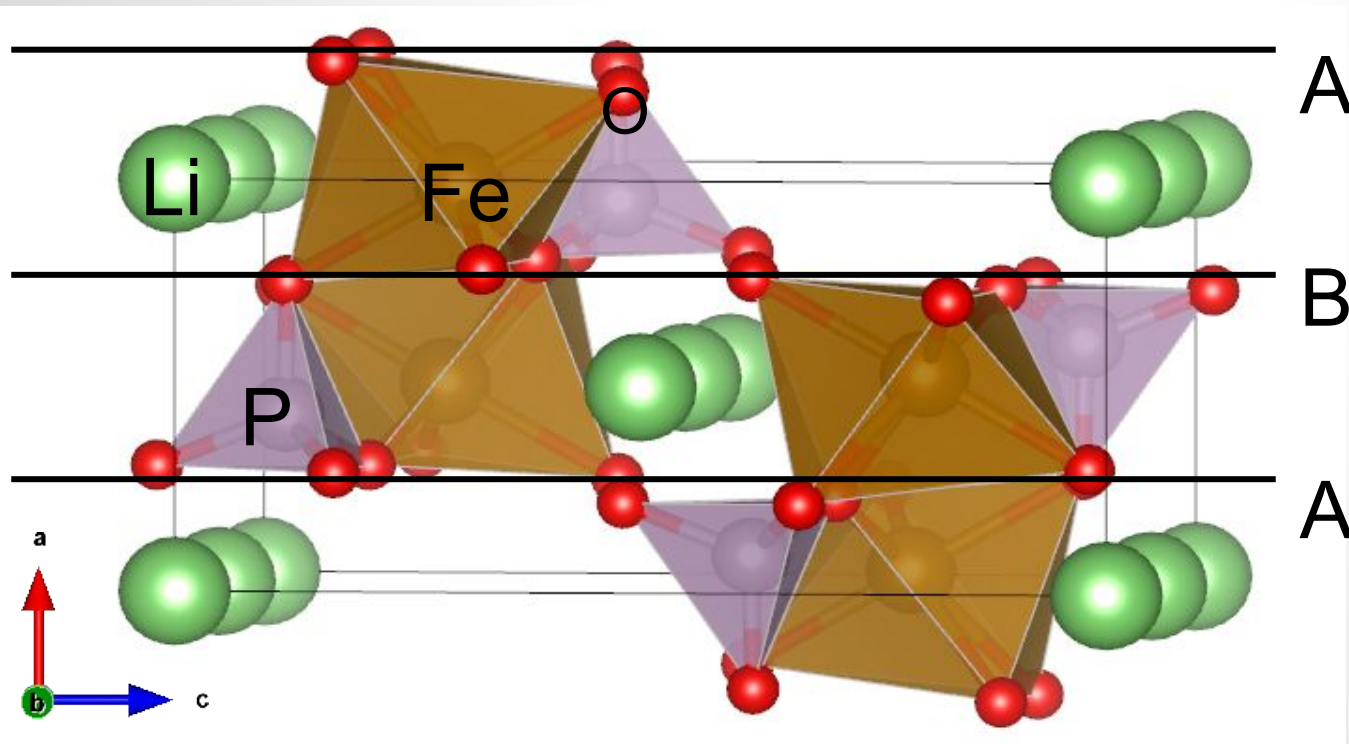


Anti-structure defect

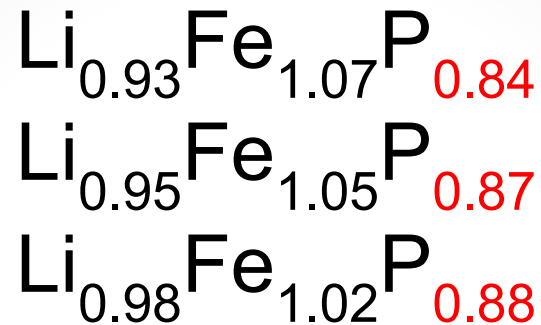
- Point defects have influence on ionic and electronic conductivity and its mechanism
- Play key role in degradation of cathode materials

Unusual point defects in LiFePO_4

Formula	name	a	b	c
LiFePO_4	triphylite	4.70	6.00	10.33

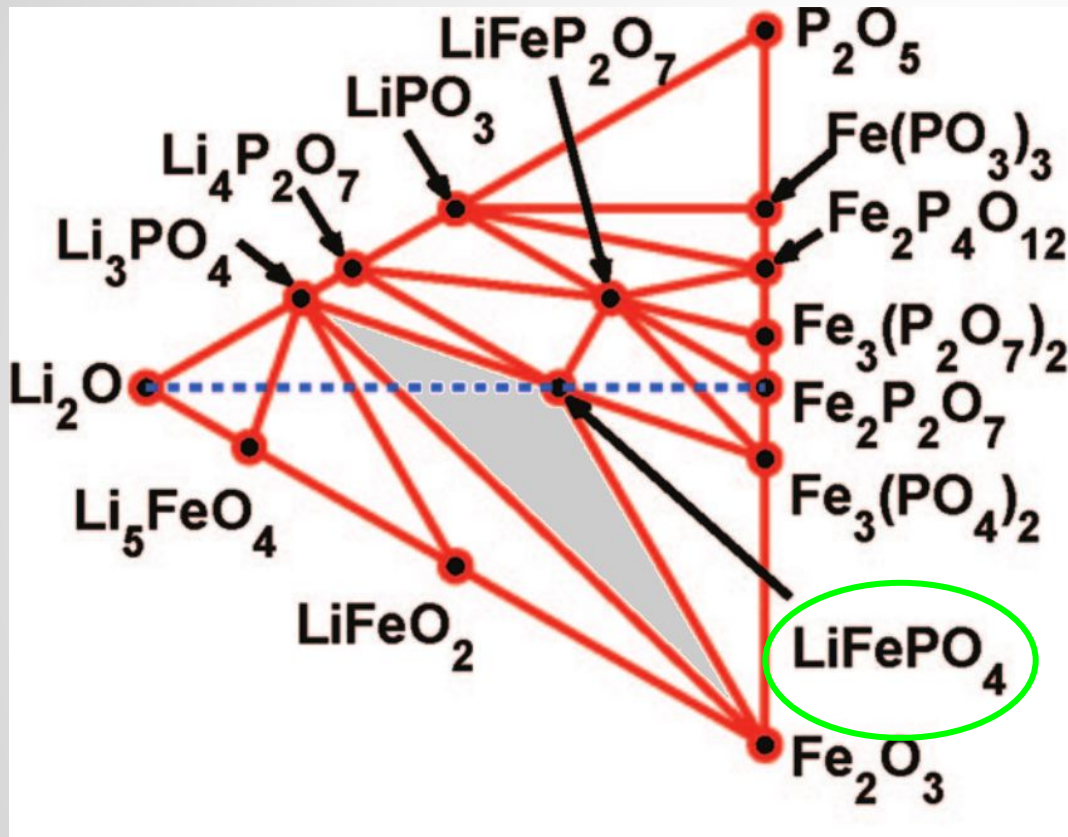


Experimentally observed compositions obtained with hydrothermal synthesis at Skoltech and MSU



Up to 16% of P vacancies!
Is it possible in LiFePO_4 ?

Li-Fe-P-O phase diagram, $\mu(\text{O}_2) = -12.4 \text{ eV}$



$\text{Li}_3\text{PO}_4 - \text{LiFePO}_4 - \text{Fe}_2\text{O}_3$ region is stable for $\mu(\text{O}_2)$ from -13.0 eV to -11.5 eV

$$\mu(\text{Fe}) = 1/2 [\mu(\text{Fe}_2\text{O}_3) - 3/2 \mu(\text{O}_2)]$$

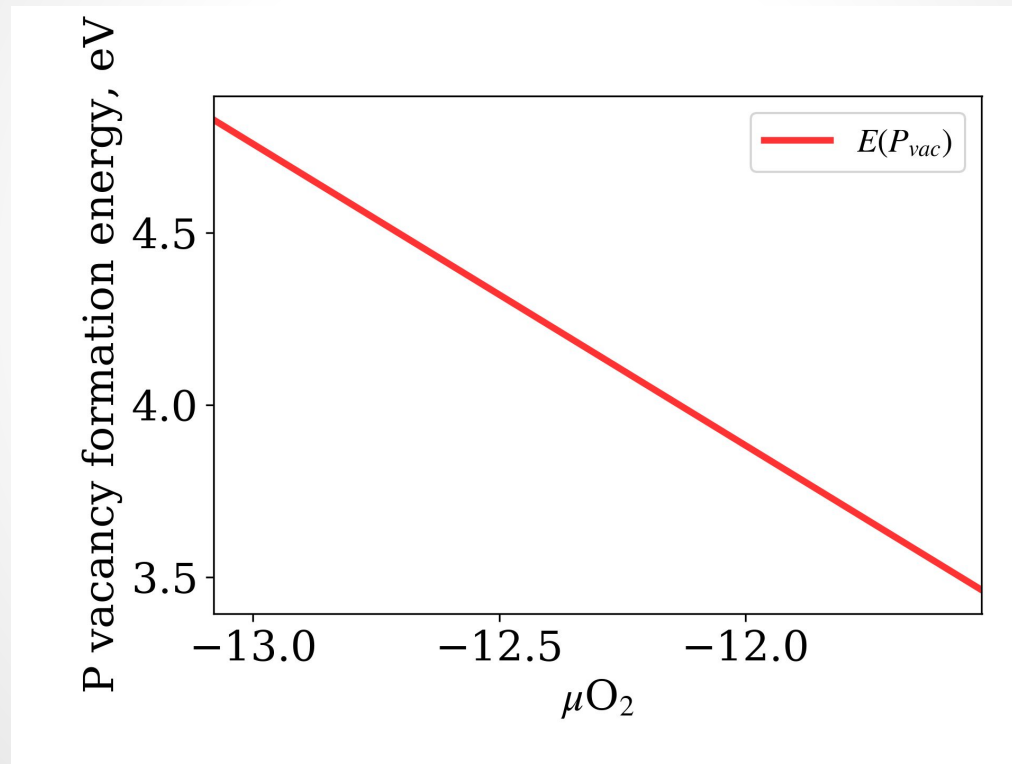
$$\mu(\text{Li}) = 1/2 [\mu(\text{Li}_3\text{PO}_4) - \mu(\text{LiFePO}_4) + \mu(\text{Fe})]$$

$$\mu(\text{P}) = 1/2 [3 \mu(\text{LiFePO}_4) - \mu(\text{Li}_3\text{PO}_4) - 3 \mu(\text{Fe}) - 4 \mu(\text{O}_2)],$$

- Ong, S.P., Wang, L., Kang, B. and Ceder, G. Li-Fe-P-O₂ Phase Diagram from First Principles Calculations. Chemistry of Materials. 20, 5 (Mar. 2008), 1798–1807.

Formation energy of P vacancies

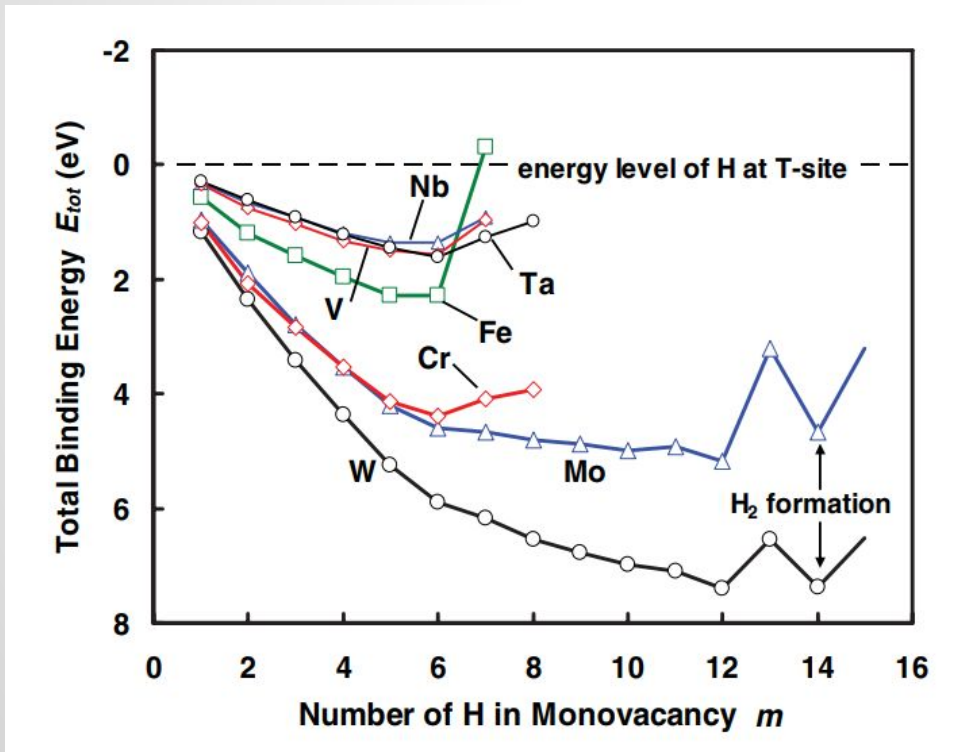
$$dE = [E(\text{LiFeP}_{1-x}\text{Vac}_x\text{O}_4) - E(\text{LiFePO}_4) + x\mu(\text{P})] / x$$



$C_{vac} = \exp(-3.5/kT) \sim 10^{-36}$ at $T = 473$ K - no vacancies are possible

How the P vacancy energy can be reduced?

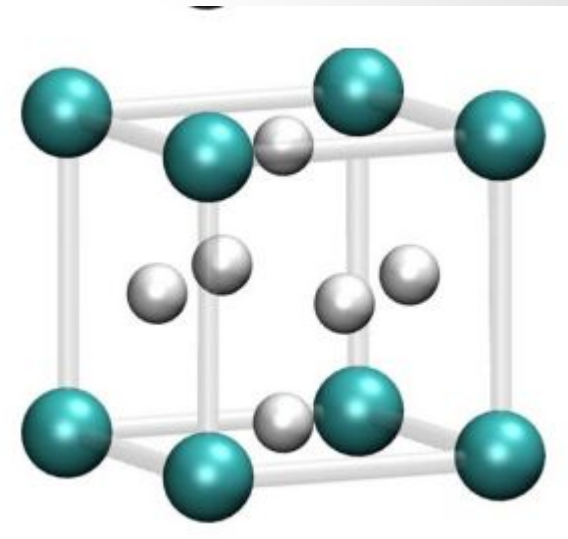
In metals, hydrogen is trapped in vacancies
E.g. in tungsten up to 12 H go into vacancy



PHYSICAL REVIEW B 85, 094102 (2012)

D. Aksenov, Skoltech

26.05.2020

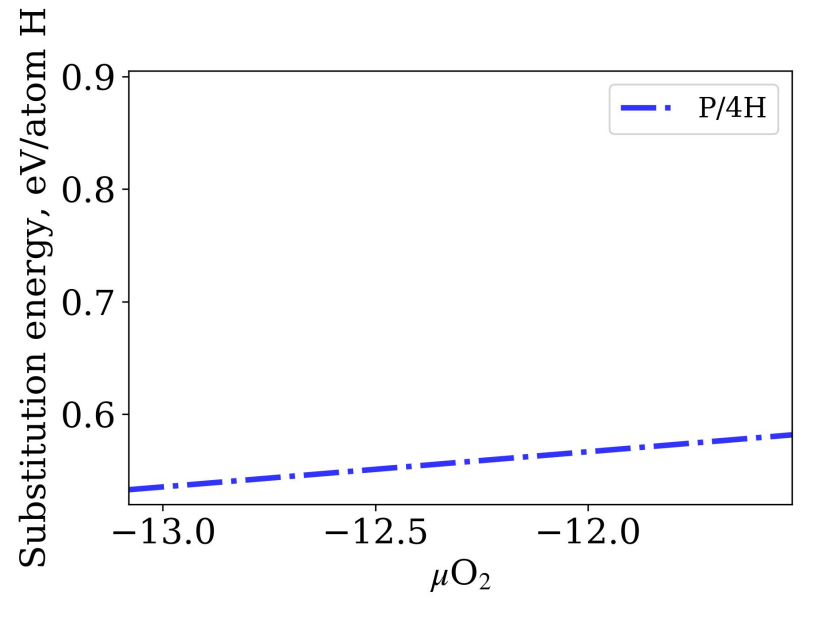
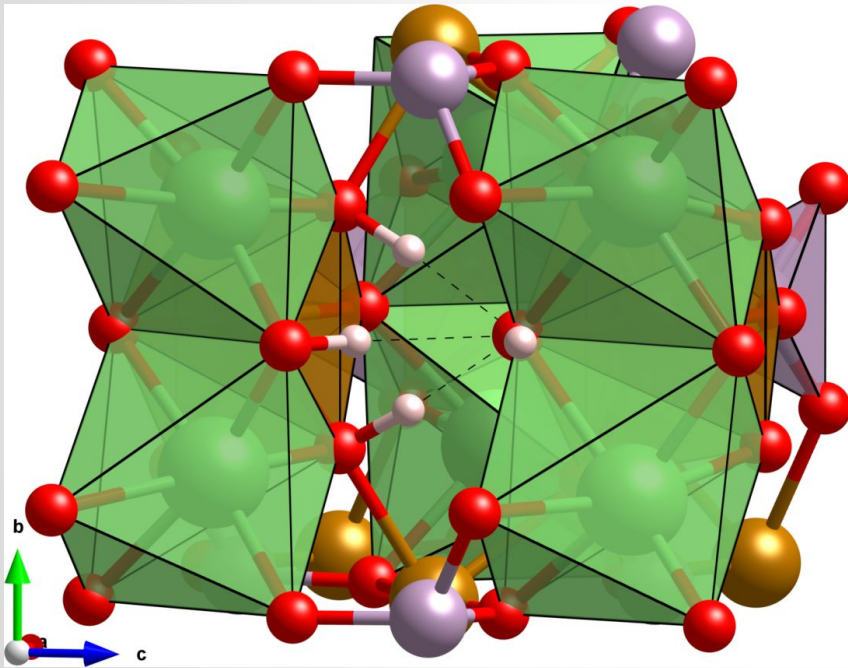


8 H in vacancy in tungsten

PHYSICAL REVIEW B 82, 094102 2010

What if 4 hydrogens substitute one P?

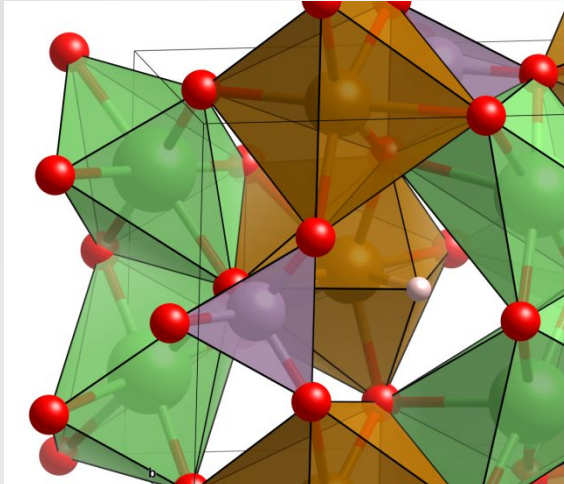
$$E_{\text{sub}} = [E(\text{LiFeP}_{1-x}\text{Vac}_x\text{H}_{4x}\text{O}_4) - E(\text{LiFePO}_4) + x\mu(\text{P}) - 4\mu(\text{H})]/4x$$



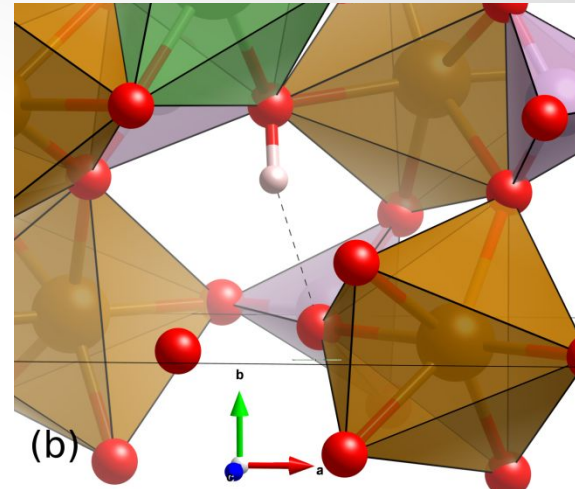
Hydrogen stabilize P vacancy reducing it's formation energy from 4.8 eV to 2.1 eV

What about other substitutions?

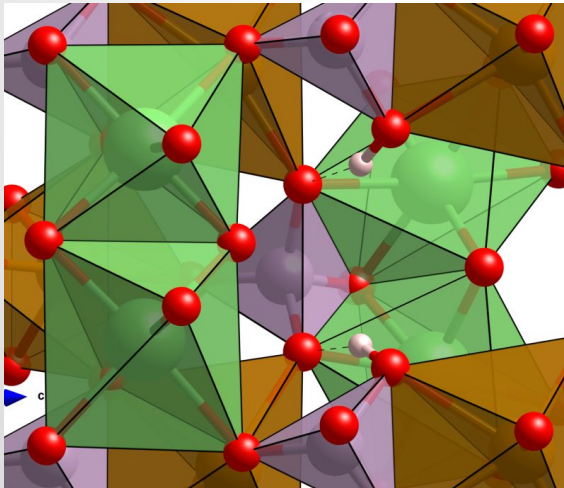
1 H in octa



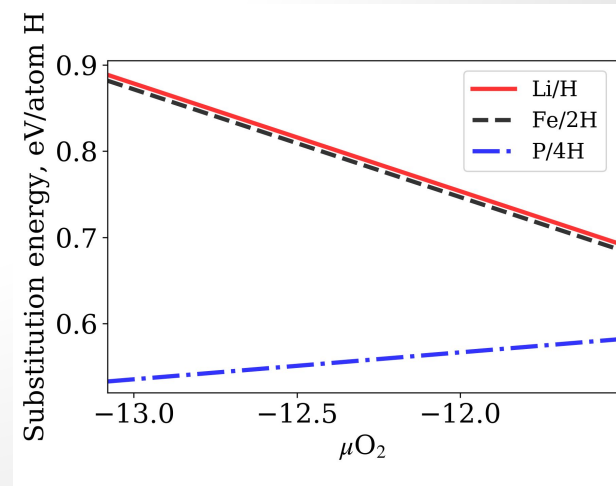
H/Li sub



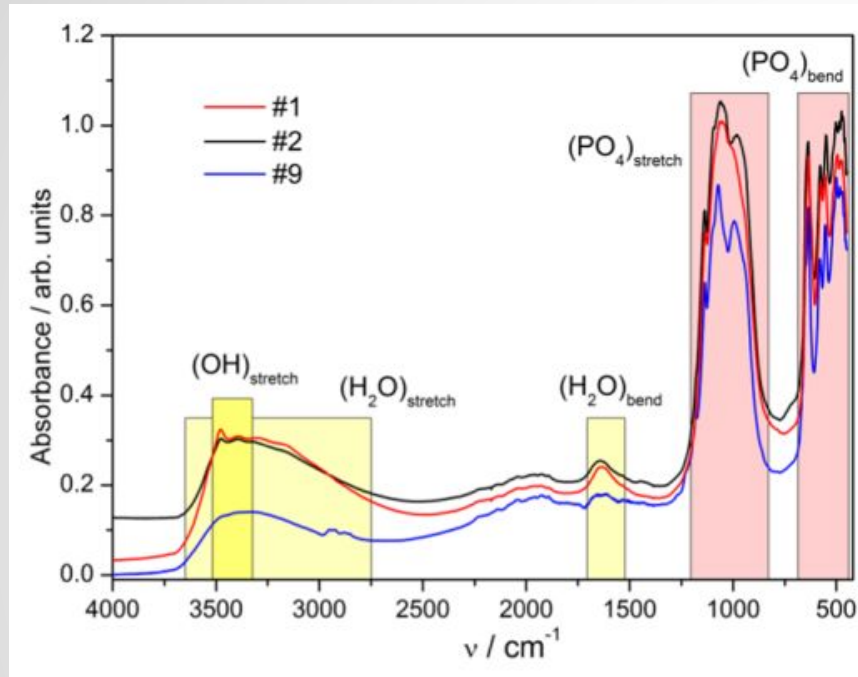
2H/Fe sub



Dependence from μ_{O_2} chemical potential



Experimental confirmation of 4H defect



- After theoretical prediction the existence of 4H defects was confirmed experimentally at our center using both Mossbauer and Infrared spectroscopy.

- However, the exact atomic structure of defect is known only from DFT calculations

Sumanov, Vasily D., Dmitry A. Aksyonov, Oleg A. Drozhzhin, Igor Presniakov, Alexey V. Sobolev, Iana Glazkova, Alexander A. Tsirlin et al. "Hydrotriphylites" $\text{Li}_{1-x}\text{Fe}_{1+x}(\text{PO}_4)_{1-y}(\text{OH})_4$ as Cathode Materials for Li-ion Batteries." *Chemistry of Materials* 31, no. 14 (2019): 5035-5046.

In mineral world hydrogarnet defect in Mg_2SiO_4 is known for a long time

Phys Chem Minerals (1983) 9:57–60

PHYSICS AND CHEMISTRY
OF MINERALS
© Springer-Verlag 1983

A Model of the OH Positions in Olivine, Derived from Infrared-Spectroscopic Investigations

A. Beran¹ and A. Putnis²

¹ Institut für Mineralogie und Kristallographie der Universität Wien, Dr. Karl Lueger-Ring 1, 1010 Vienna, Austria

² Department of Earth Sciences, University of Cambridge, Downing Street, Cambridge CB2 3EQ, England

- First experimental evidence of hydrogarnet type defect in olivine was obtained by Beran and Putnis in **1983** (though P/3H)
- DFT calculations for P/4H in Mg_2SiO_4 was done in **2000** by Brodholt and Refson

JOURNAL OF GEOPHYSICAL RESEARCH, VOL. 105, NO. B8, PAGES 18,977–18,982, AUGUST 10, 2000

An ab initio study of hydrogen in forsterite and a possible mechanism for hydrolytic weakening

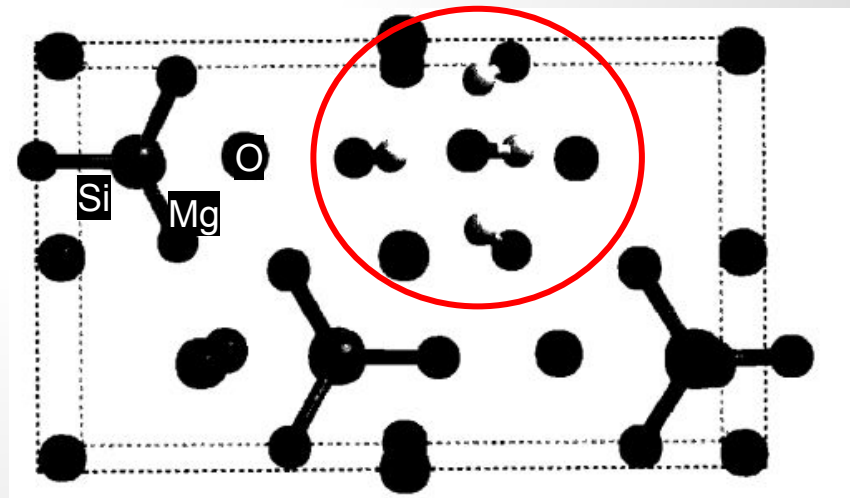
John P. Brodholt

Department of Earth and Planetary Sciences, University College London, London

Keith Refson

Department of Earth Science, University of Oxford, Oxford, England

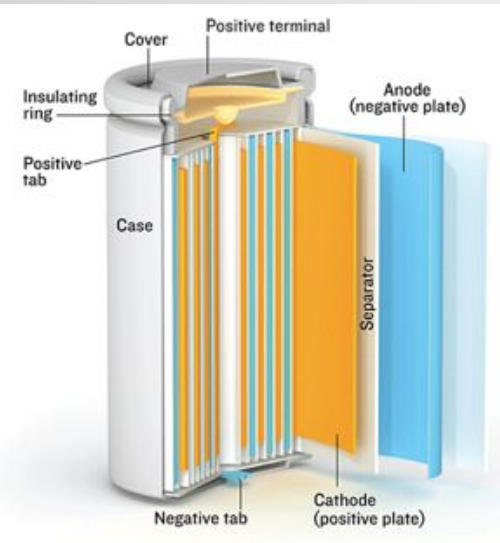
Abstract. Even small amounts of water can profoundly effect the physical properties of minerals. In olivine <1 H in every 1000 unit cells acts to increase creep rates of dunite by ~ 2 orders of magnitude. Although the mechanism for this is not known, it is not unreasonable to suggest that it is in some way related to an increase in the point defect population. In order to understand this better we have performed ab initio pseudopotential calculations within the generalized gradient approximation on protonic defects in Mg_2SiO_4 forsterite. Three mechanisms for incorporating protons are considered: (1) interstitial, (2) binding at cation vacancies, and (3) binding at silicon vacancies. Assuming the existence of both Si



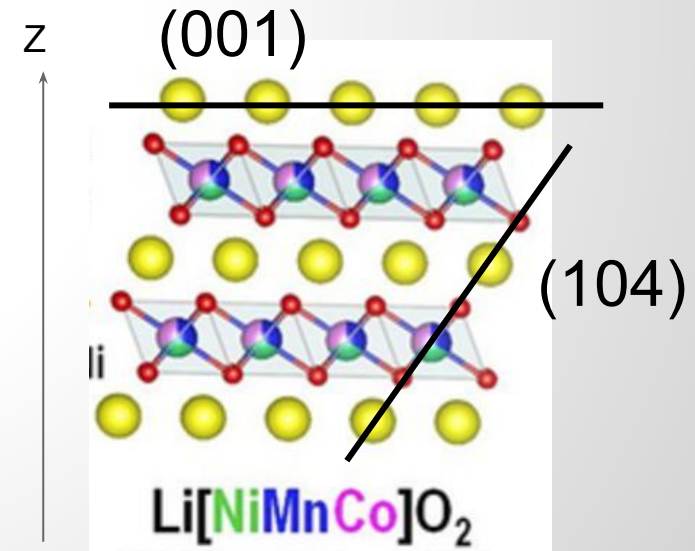
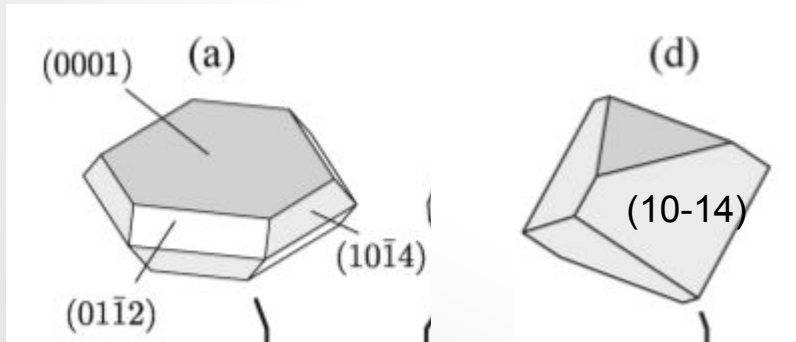
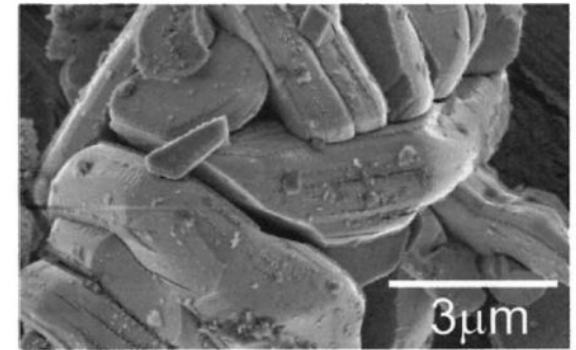
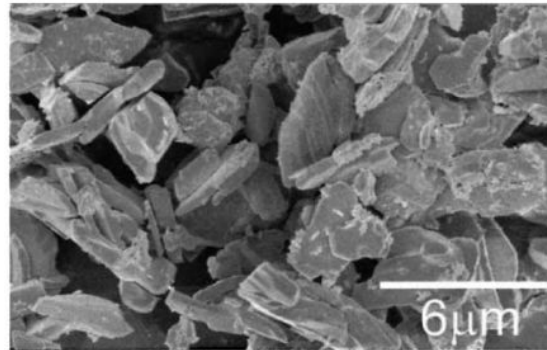
Outline

- 1. Motivation to study energy materials and introduction into battery components*
- 2. Modeling of solid electrodes*
- 3. Modeling of electrolytes and interfaces*
- 4. High-throughput modeling*
- 5. Few examples from our experience: OH defects in LiFePO_4 , antisite defects in layered oxides, migration barriers in cathodes*

Morphology and surface structure of cathode particles is highly important!



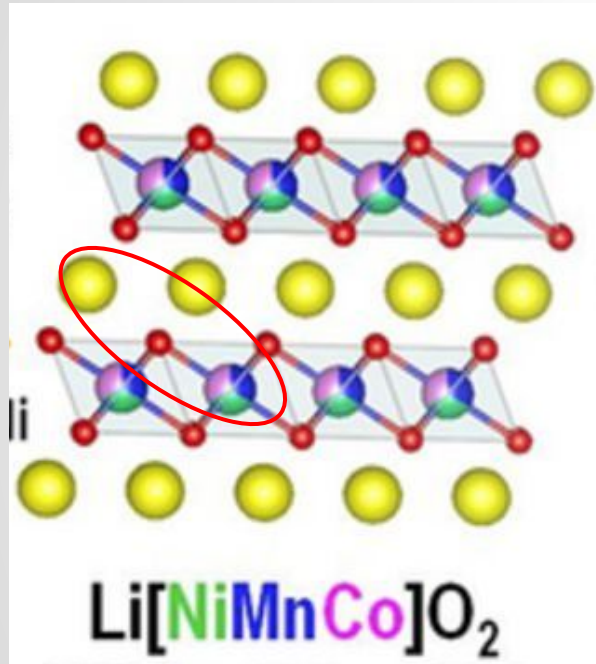
(b) O₂-LiCoO₂



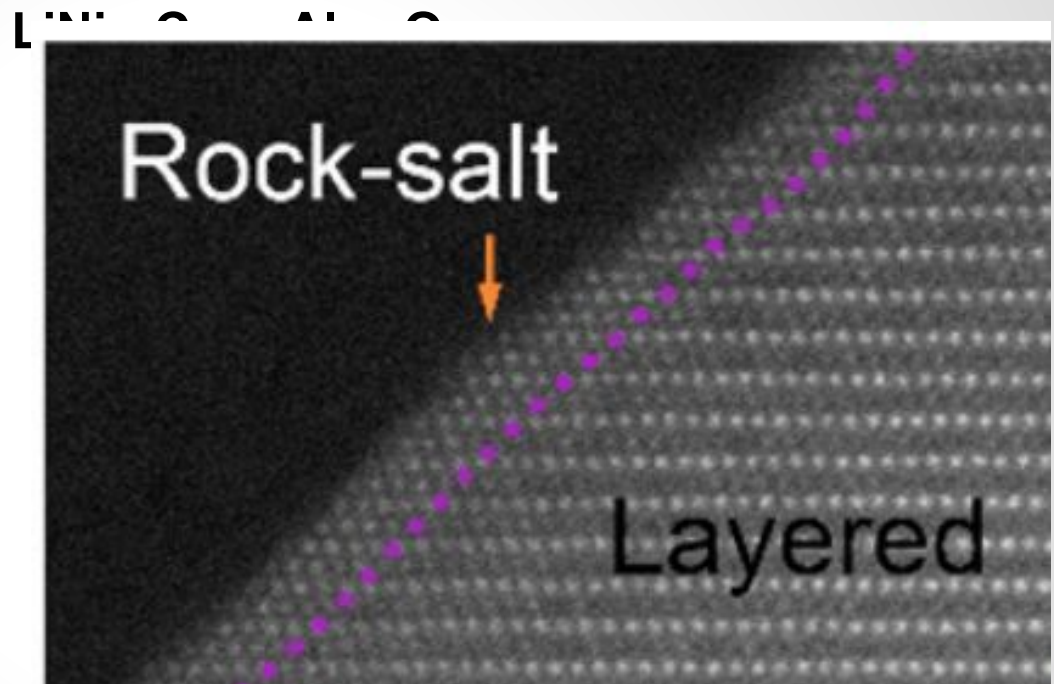
Carlier2001 Kramer2009

What happens on the surface?

Rocksalt-type surface reconstruction



TEM of (104)



$(104)\text{hex} \rightarrow (002)\text{cubic}$

Zhang2018

Main question

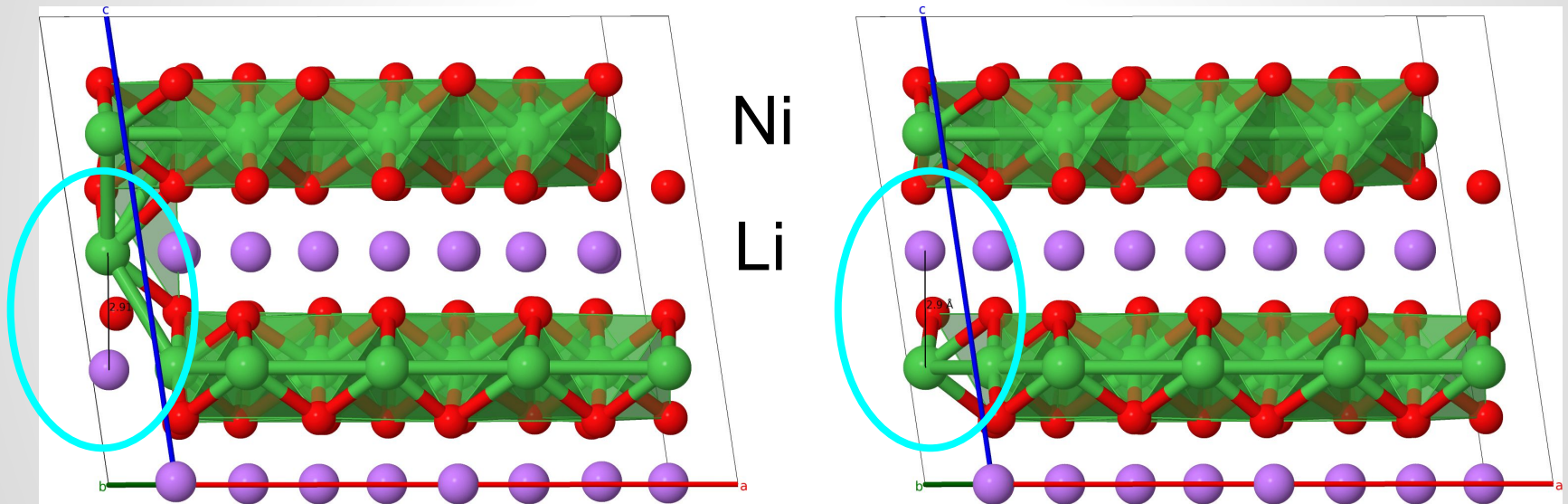
Is surface reconstruction based on antisite pairs kinetically controlled or any thermodynamic driving force exists?



Make DFT+U atomic simulation neglecting the influence of electrolyte.

Formation energy of antisites

Very important type of defects in layered oxides, up to 10% in LiNiO_2 , but much smaller in LiCoO_2



$$dE_{AS} = E(\text{supercell with antisite}) - E(\text{ideal supercell})$$

Siman code: creating antisite defects

```
In [12]: NCO = smart_structure_read('geo/POSCAR_NaCoO2')
         create_antisite_defect(NCO, 'Na', 'Co', max_sep = 6, iatom = 1)
```

-- List of antisites:

No.	Antisite type	at1	at2	Separation, A
0	(0, 32)	2	35	3.091
1	(0, 32)	2	34	4.247
2	(0, 32)	2	33	5.15

Antisite pairs formation energies

Phase	space group	AS energy
LiNiO ₂	R-3m	- 0.8 eV
LiCoO ₂	R-3m	1.9 eV
NaNiO ₂	C2/m	2.1 eV
NaCoO ₂	R-3m	2.9 eV

Negative antisite formation energy for LiNiO₂!

May be the problem with LiNiO_2 space group?

- LiNiO_2 is often reported in **R-3m** group, where all Ni-O bonds are fixed to 1.99 Å.
- However Jahn-Teller (**JT**) distortion and charge ordering of Ni^{3+} to Ni^{2+} and Ni^{4+} are possible with the reduction of energy

LiNiO₂ in P2/c with charge order is most stable

PHYSICAL REVIEW B **84**, 085108 (2011)

Charge disproportionation and Jahn-Teller distortion in LiNiO₂ and NaNiO₂: A density functional theory study

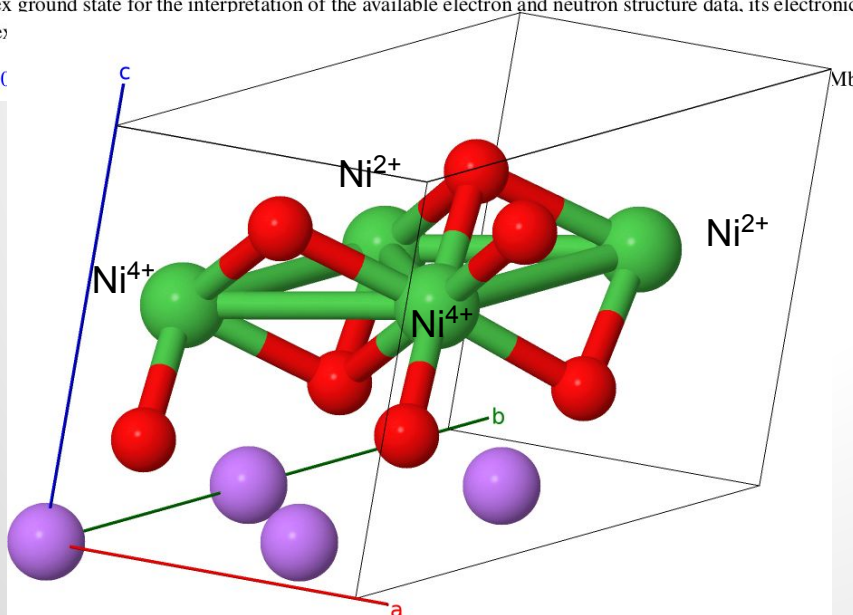
Hungru Chen,^{*} Colin L. Freeman, and John H. Harding

Department of Materials Science and Engineering, University of Sheffield, S1 3JD, United Kingdom

(Received 24 March 2011; revised manuscript received 12 July 2011; published 19 August 2011)

Density functional theory calculations have been performed on three potential ground-state configurations of LiNiO₂ and NaNiO₂. These calculations show that, whereas NaNiO₂ shows the expected cooperative Jahn-Teller distortion (and therefore a crystal structure with *C2/m* symmetry), LiNiO₂ shows at least two possible crystal structures very close in energy (within 3 meV/formula unit): *P2₁/c* and *P2/c*. Moreover, one of them (*P2/c*) shows charge disproportionation of the (expected) Ni³⁺ cations into Ni²⁺ and Ni⁴⁺. We discuss the implications of this complex ground state for the interpretation of the available electron and neutron structure data, its electronic and complex

DOI: 10.1103



- Charge-disproportionation of Ni³⁺ to Ni²⁺ and Ni⁴⁺
- According to our results the total energy reduced by **15 meV/atom**

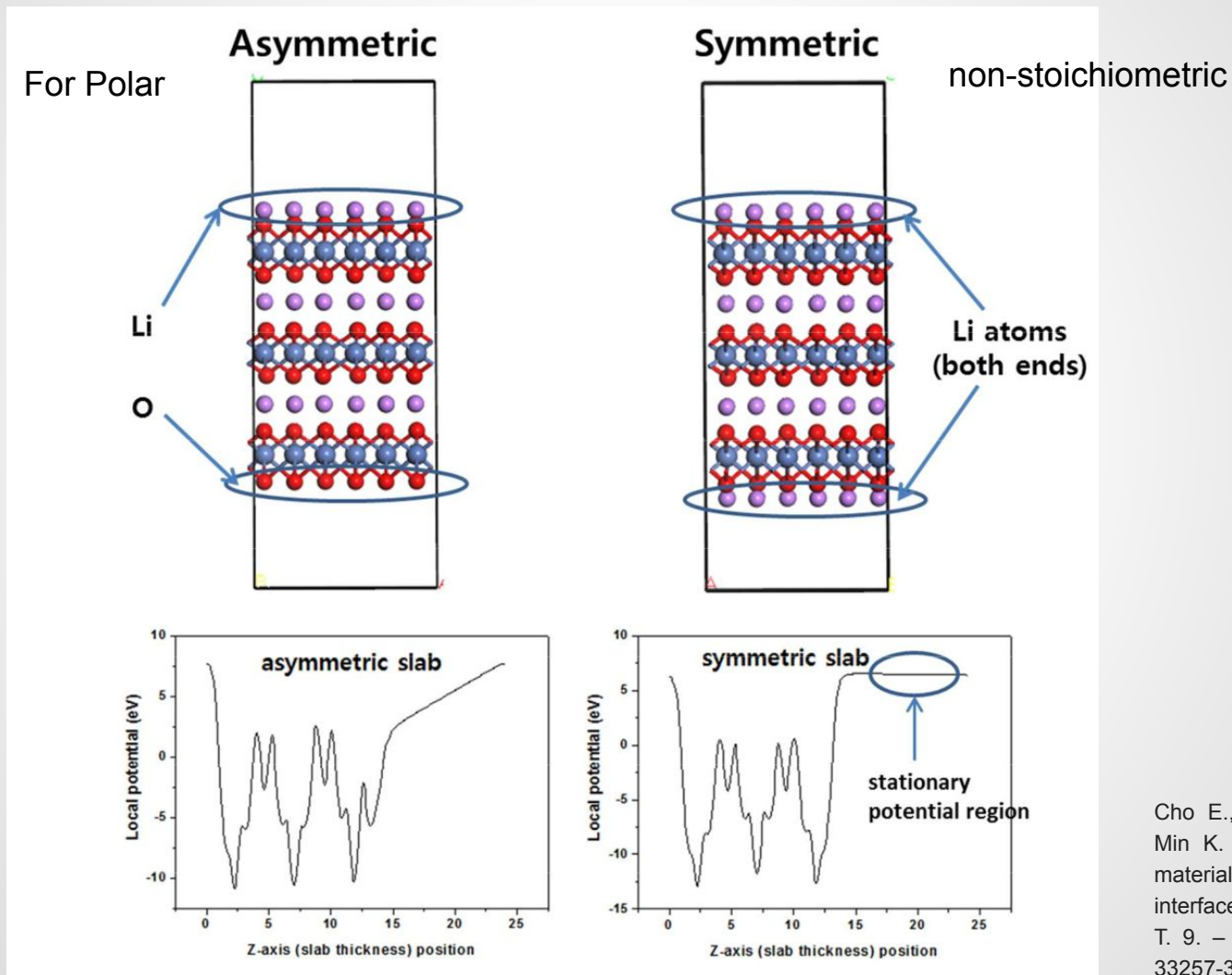
- 1.5 eV for 100-atom cell!

Antisite pairs formation energies

Phase	space group	AS energy	NN, sep, A
LiNiO ₂	P2/c	0.73 eV (0.75 [1])	1nn, 2.86 A
LiCoO ₂	R-3m	1.9 eV	1nn, 2.82 A
NaNiO ₂	C2/m	2.1 eV	2nn, 4.17 A
NaCoO ₂	R-3m	2.9 eV	2nn, 4.22 A

Chen, Hungru, James A. Dawson, and John H. Harding. "Effects of cationic substitution on structural defects in layered cathode materials LiNiO₂." *Journal of Materials Chemistry A2*, no. 21 (2014): 7988-7996.

Surface energy calculations



Cho E., Seo S. W.,
Min K. ACS applied
materials &
interfaces. – 2017. –
T. 9. – №. 38. – C.
33257-33266./SI

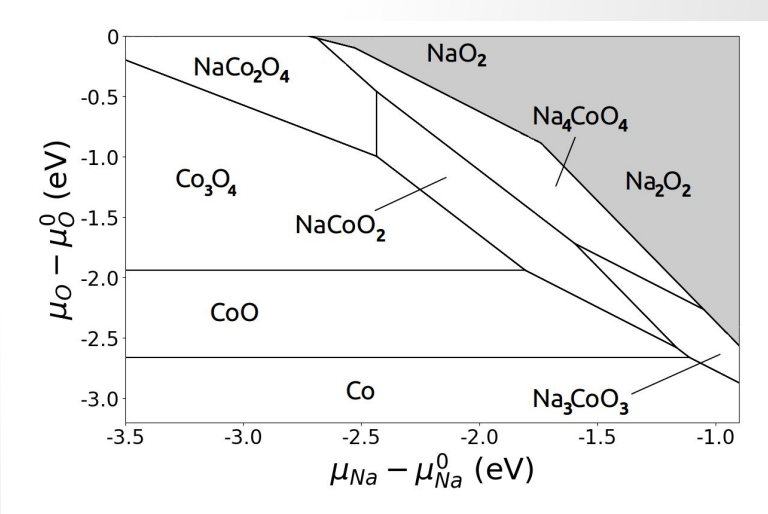
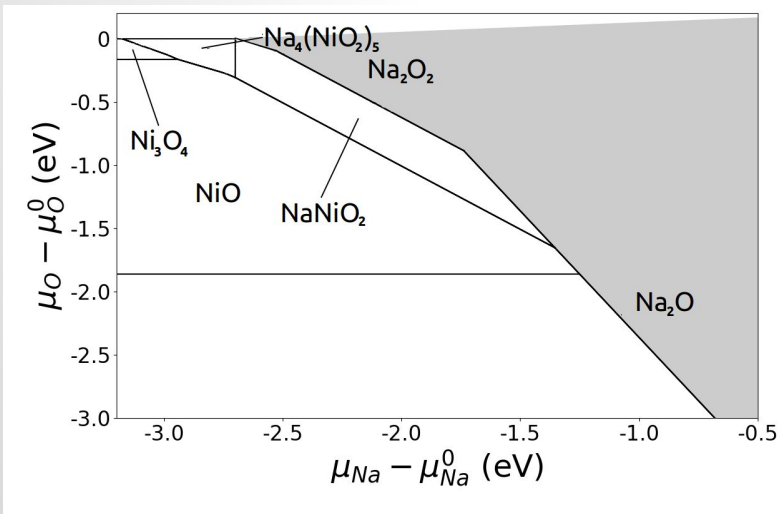
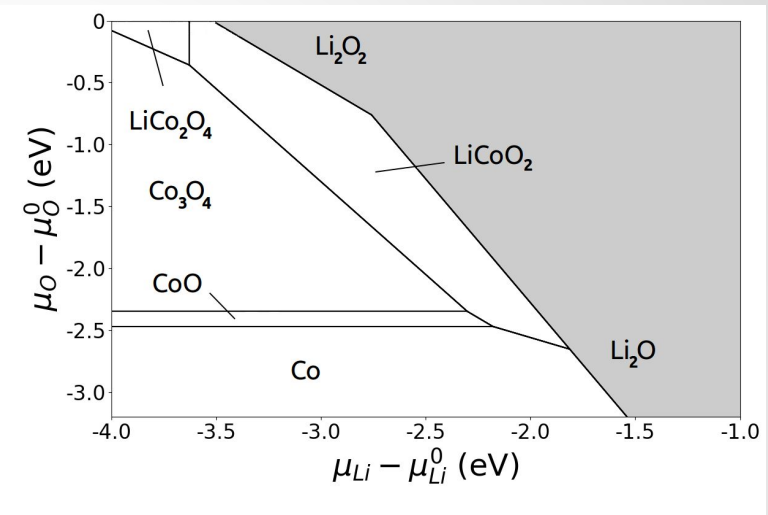
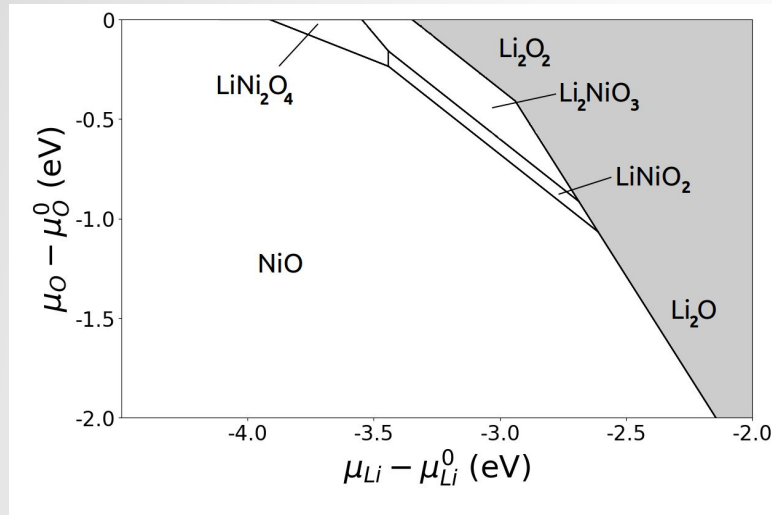
Surface energies

$$\gamma = \frac{1}{2 \cdot A} \left[E_{\text{slab}} - N_{\text{Co}} \left(\varepsilon_{\text{b}} - \sum_i \Gamma_i \cdot \mu_i \right) \right]$$

ε_{b} is energy of bulk cell, Γ_i is excess of i atoms in the slab

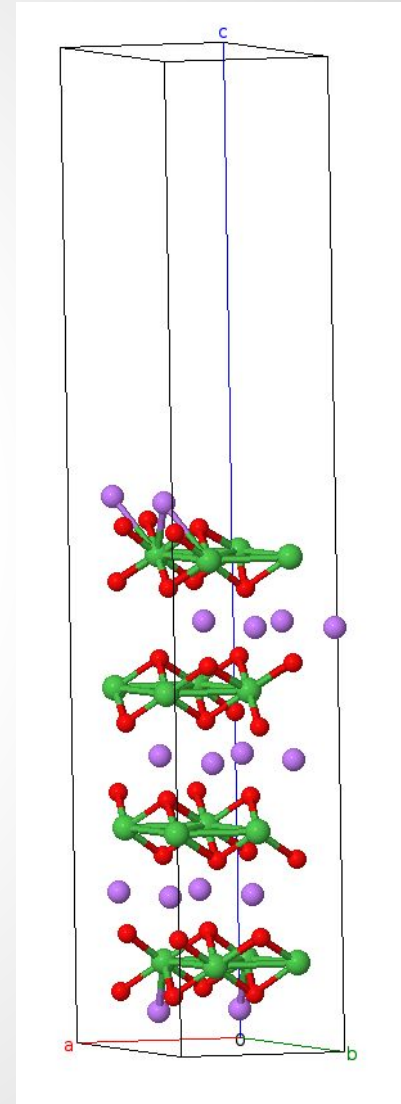
Dependence on chemical potential !
phase diagram is required

Phase diagrams in chemical potential space



SIMAN: creating slabs with surfaces

```
1 st = create_surface2(sc, [0, 0, 1],  
    cut_thickness = 10, min_vacuum_size = 10,  
    symmetrize = 0, min_slab_size = 16)
```



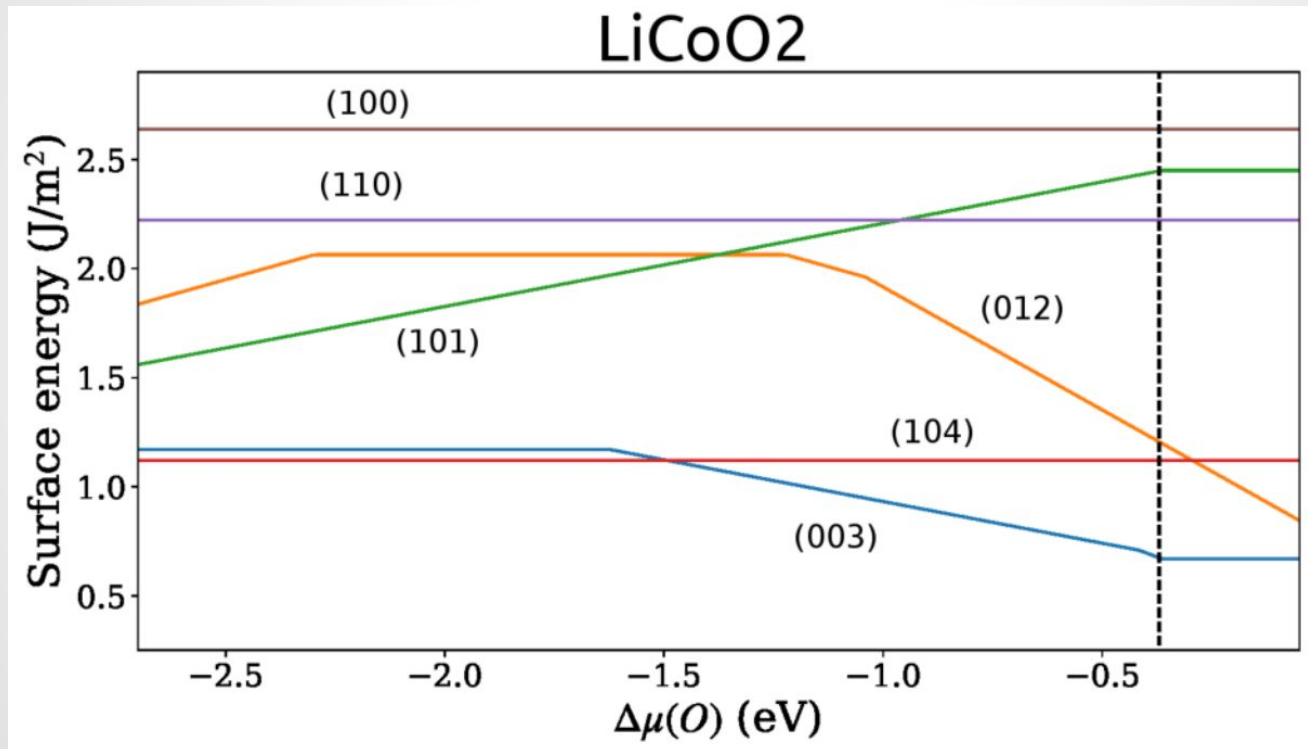
Surface energy (J/m²) of considered oxides

Surface	LiNiO ₂ (R-3m)	LiCoO ₂ (R-3m)	NaNiO ₂ (C2/m)	NaCoO ₂ (R-3m)
(001) ½ ML	0.65	1.2	1.35	1.35
(104)/ (10-1)	0.55	1.1	0.35	0.87

Considered surfaces, example of LiCoO_2

R-3m: non-polar (104), (110), (100), polar : (012), (003), (101), (111)

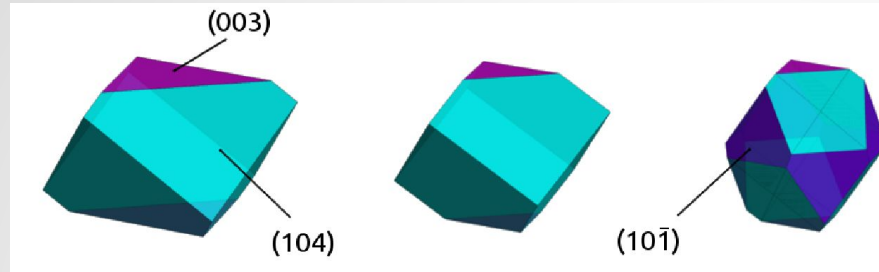
C2/m: non-polar (104), (10-1), (100), (111), (10-2); polar - (003), (012), (110)



Dependence of surface energy on chemical potential

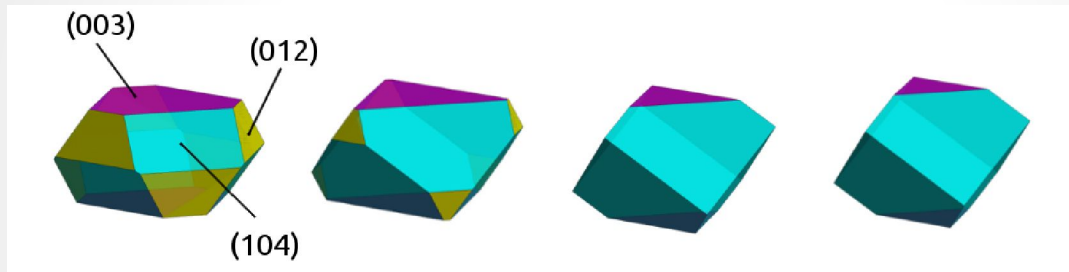
Wulff construction depending on chemical potential

LiNiO_2

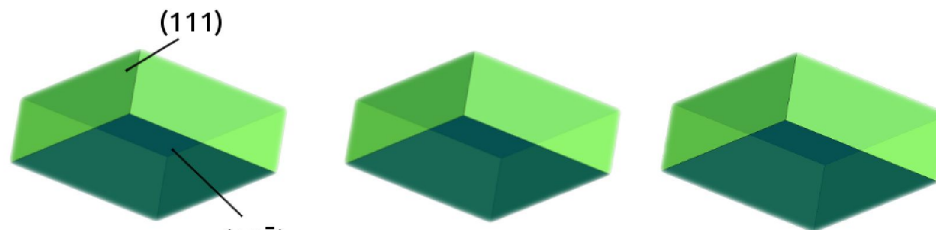


Wulff construction - minimizes the total surface energy for a given particle volume

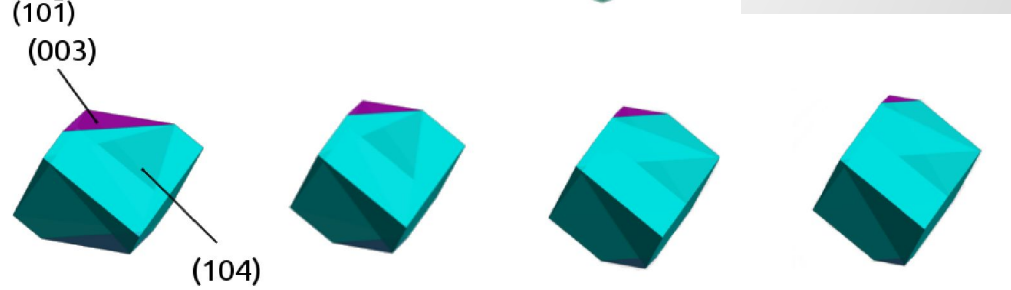
LiCoO_2



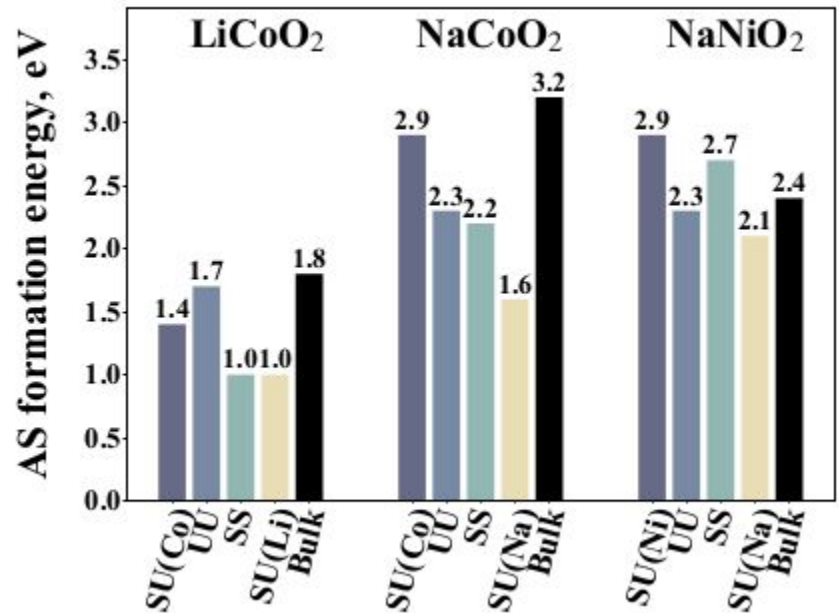
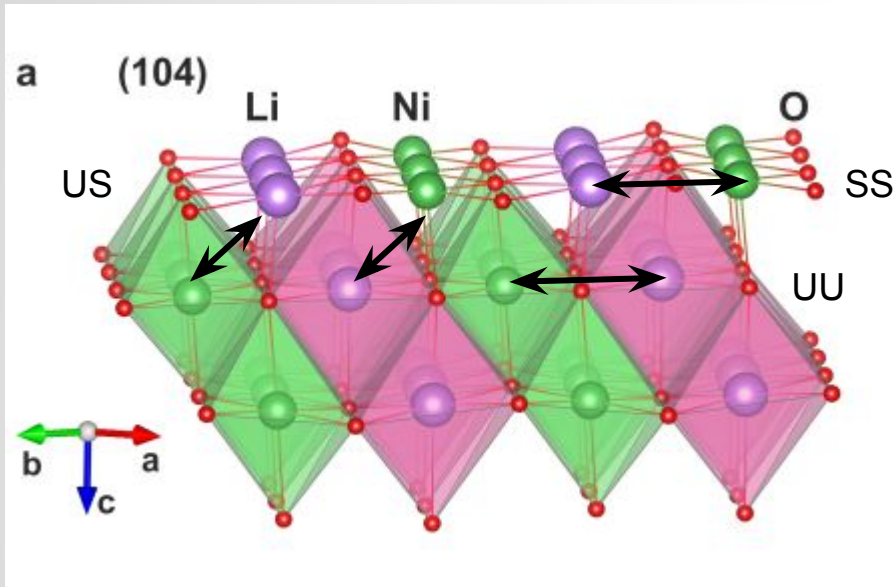
NaNiO_2



NaCoO_2



Surface antisites



In Co-based oxides surface antisite pair is formed more easily, however the energy is still positive

- Influence of electrolyte?
- Kinetic control?
- Chemical composition change?

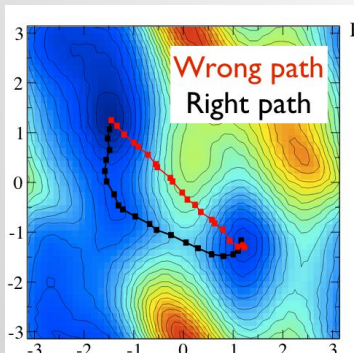
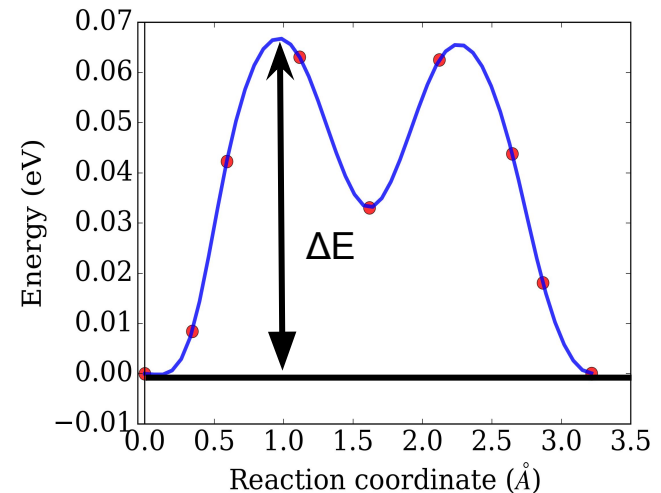
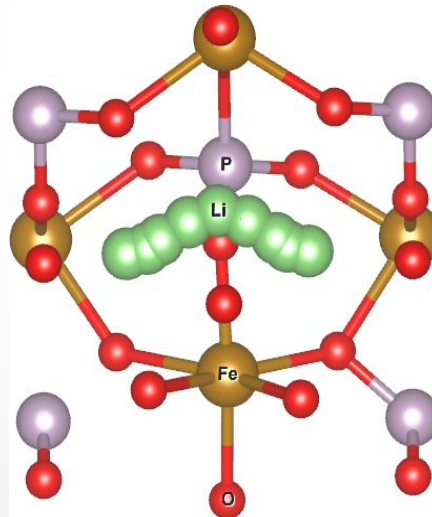
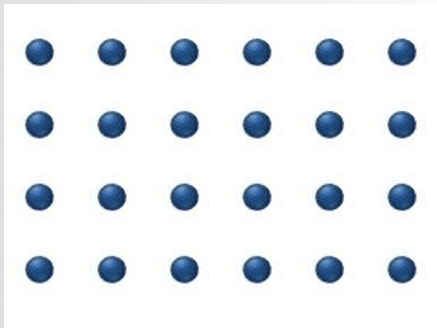
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- 4. High-throughput modeling*
- 5. Few examples from our experience: OH defects in LiFePO_4 , antisite defects in layered oxides, migration barriers in cathodes*

Case study: migration barriers in cathodes

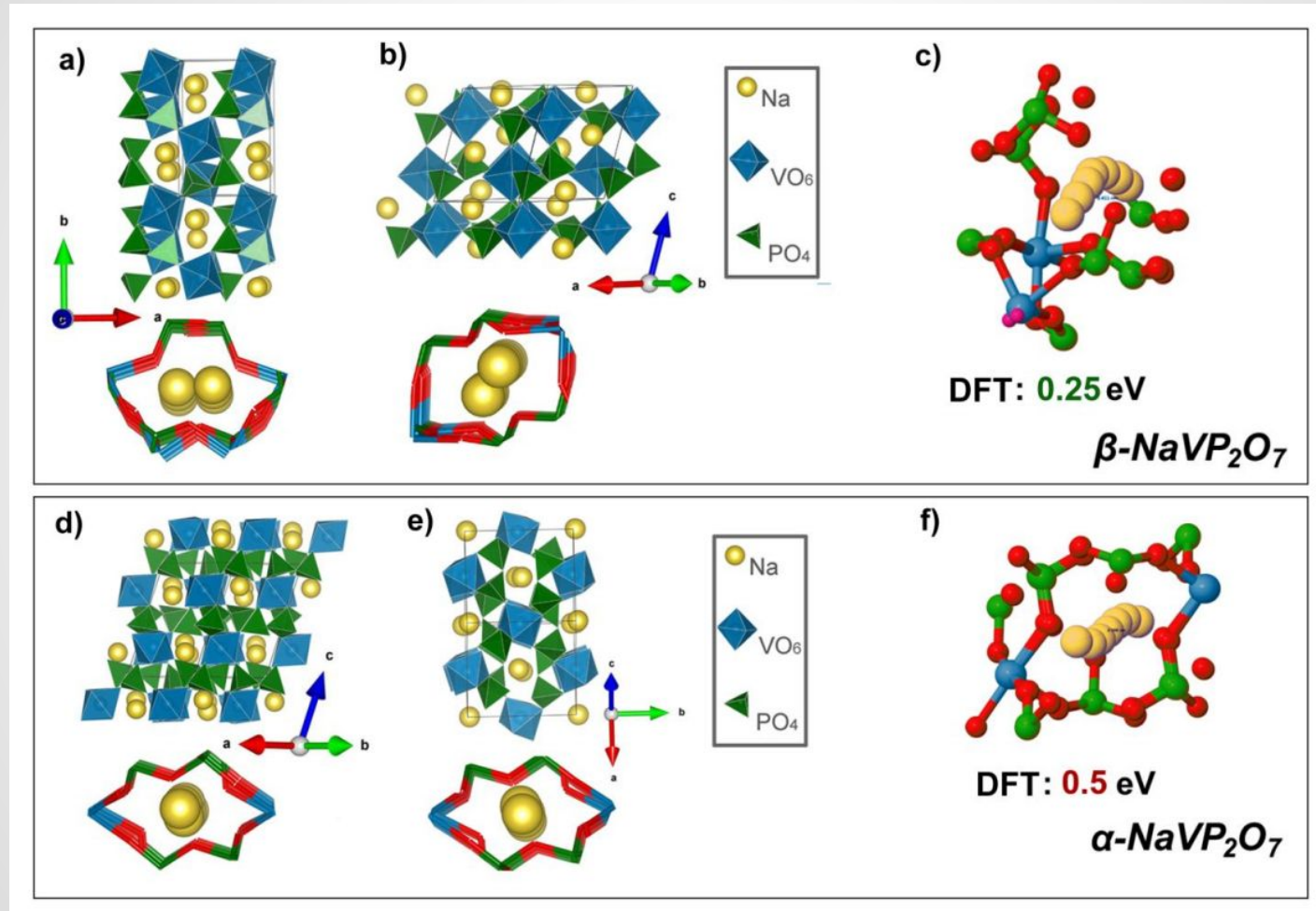
- **Ionic** and electronic conductivity of electrodes determines C-rate
- Ionic conductivity depends on diffusivity of cations
- Migration barrier should be less 0.3-0.4 eV

$$D = 1/2\Gamma d^2 \quad \Gamma = \nu^* \exp\left(\frac{-\Delta E}{k_B T}\right)$$



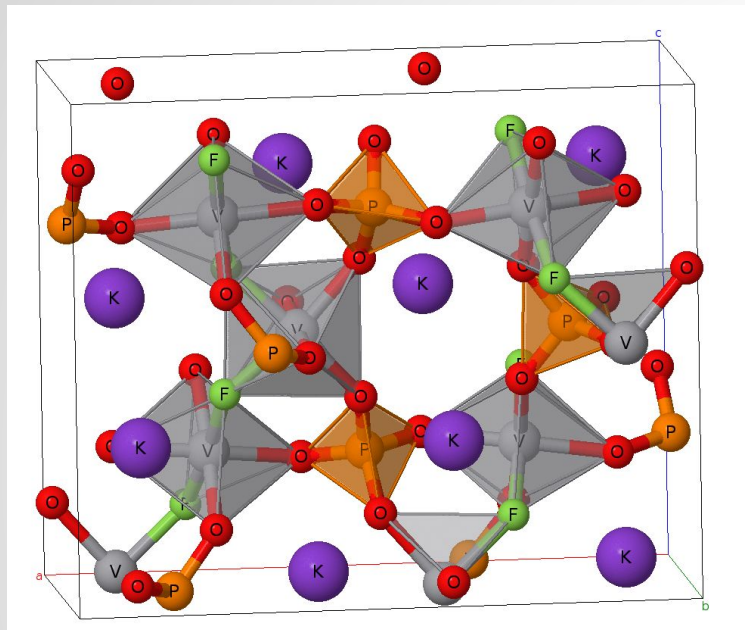
- Migration barrier can be calculated with Nudge elastic band method (NEB)

Migration of Na in NaVP_2O_7

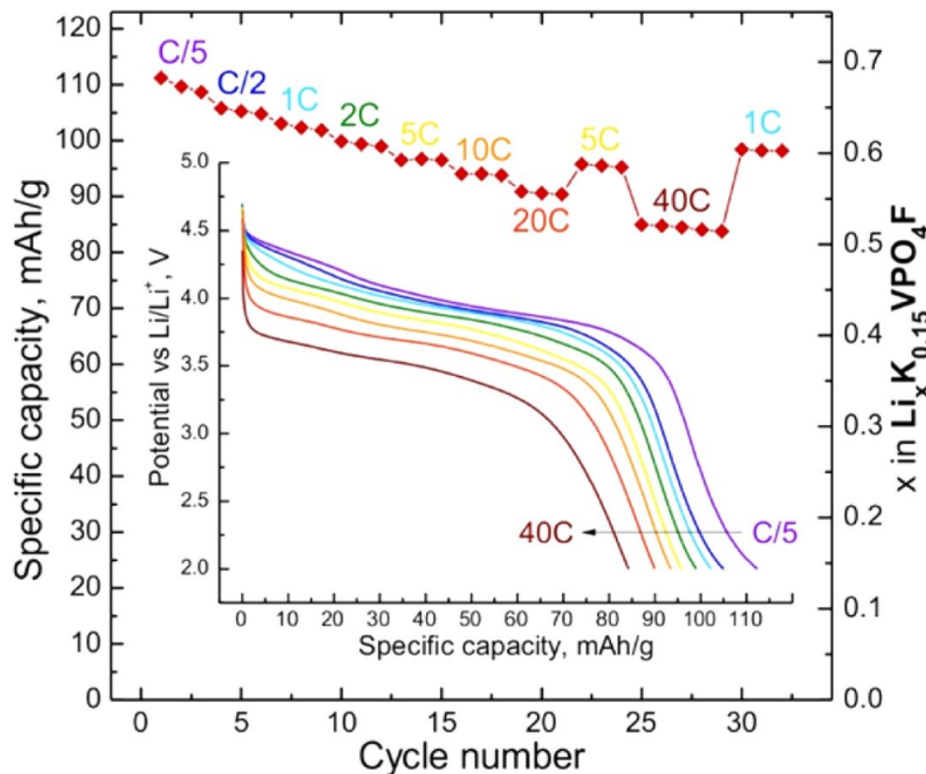


Drozhzhin, O.A., Tertov, I.V., Alekseeva, A.M., **Aksyonov, D.A.**, Stevenson, K.J., Abakumov, A.M. and Antipov, E.V., // *Chemistry of Materials*, 2019

KVPO₄F - new cathode materials developed by at MSU and Skoltech



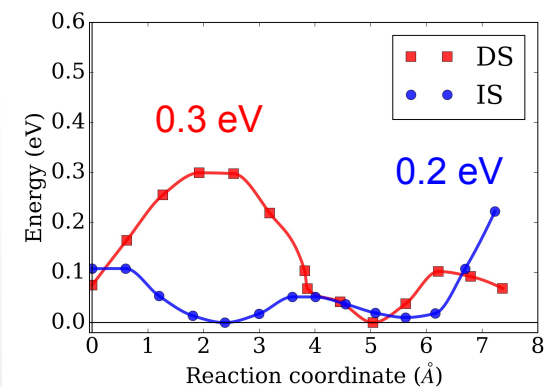
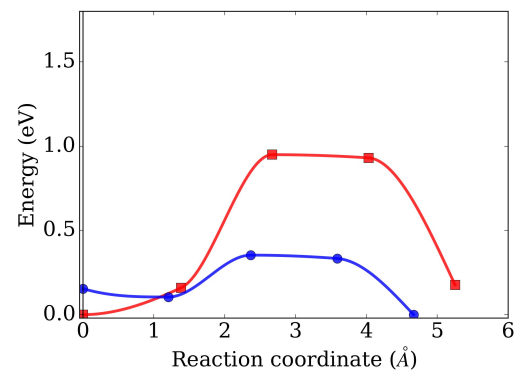
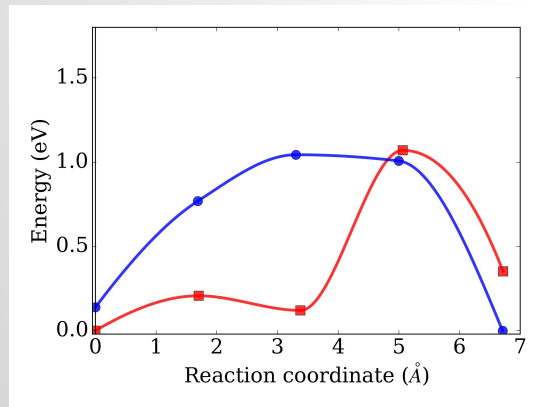
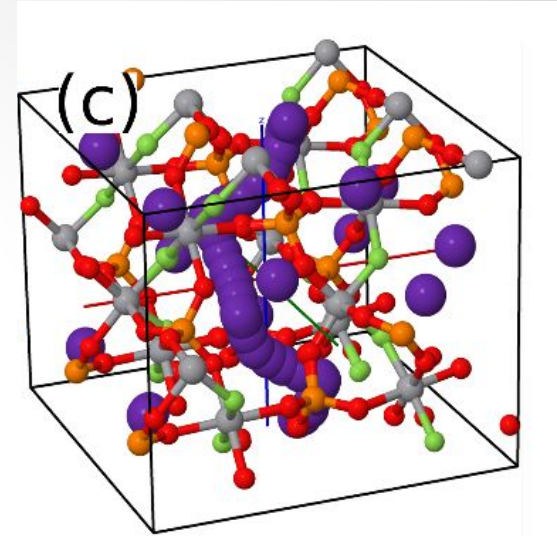
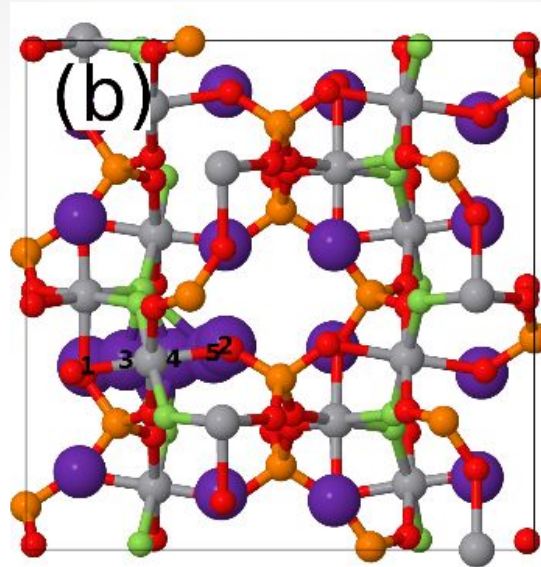
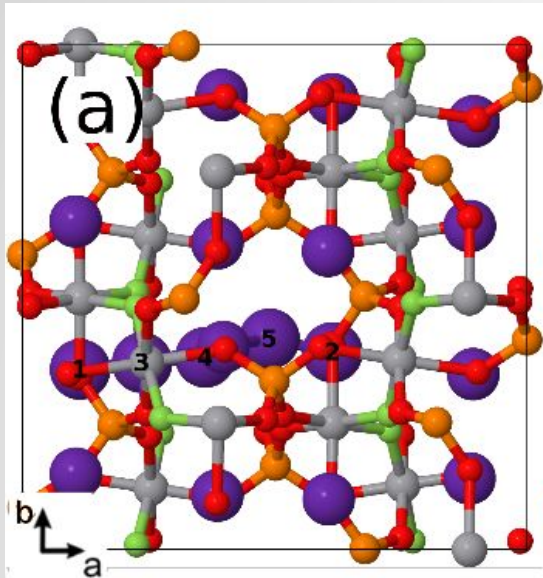
- Relatively low cost
- Possible intercalation of Li, Na, and K
- High intercalation voltage 4 V
- Very high specific rate



75 % of initial capacity at 40C

Fedotov, Stanislav S., et al. "AVPO₄F (A= Li, K): a 4 V cathode material for high-power rechargeable batteries." *Chemistry of Materials* 28.2 (2016): 411-415.

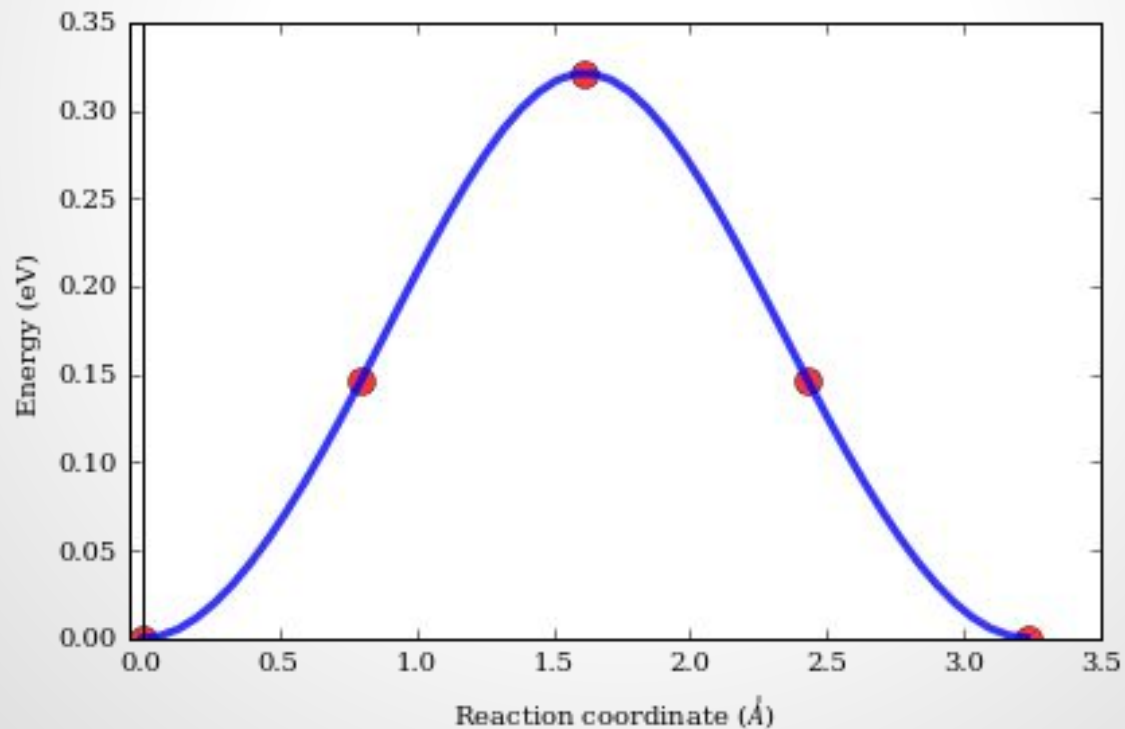
Migration in $KVPO_4F$ (IS) and VPO_4F (DS)



NEB calculation in SIMAN

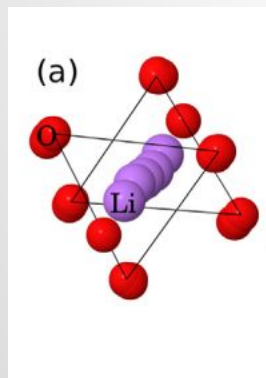
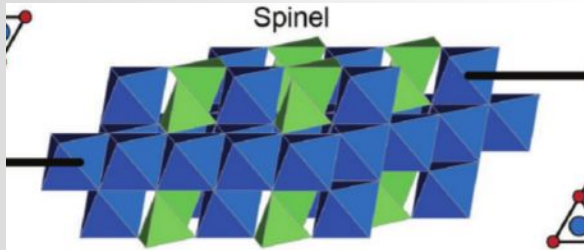
```
1 add_neb(st = st, it_new = 'LiFePO4', ise_new = 'ion_relax', it_new_folder = 'LiFePO4/neb', images = 3)
```

```
1 res('LiFePO4.n3Li1v1', 'ion_relax', [1,2,3,4,5], show = 'fomepp', analys_type = 'neb')
```

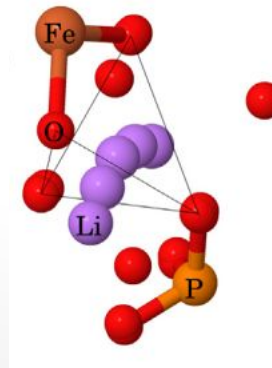
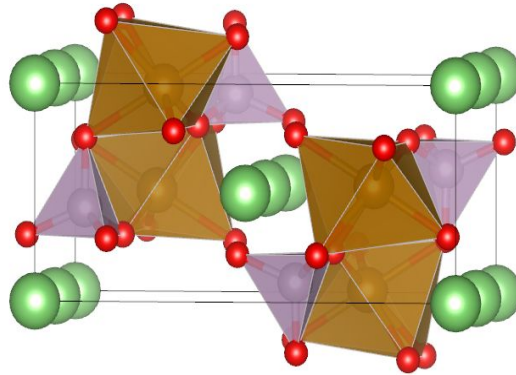


Three classes of cathodes are considered

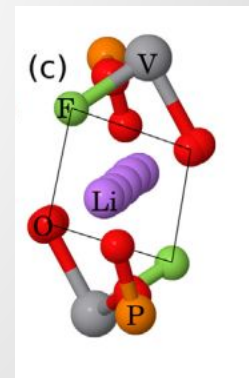
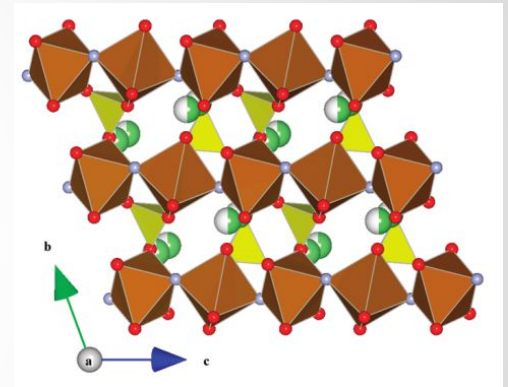
Spinel, LiMn_2O_4



Olivine, LiFePO_4 ,
 LiMnPO_4

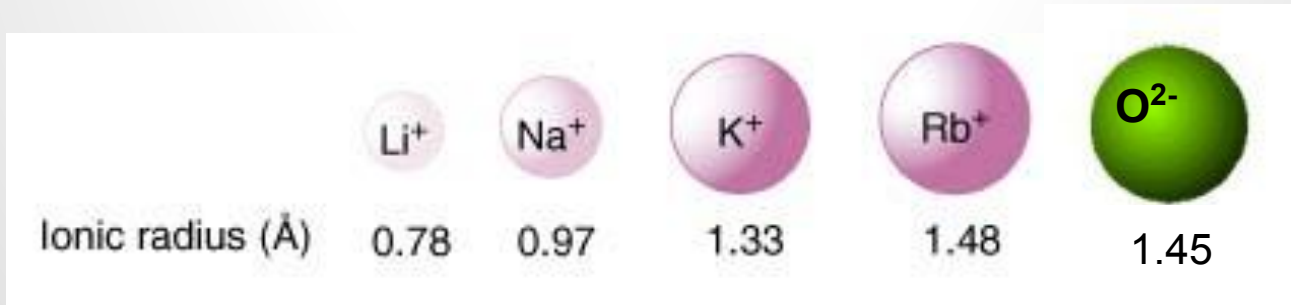







Tavorite, LiVPO_4F



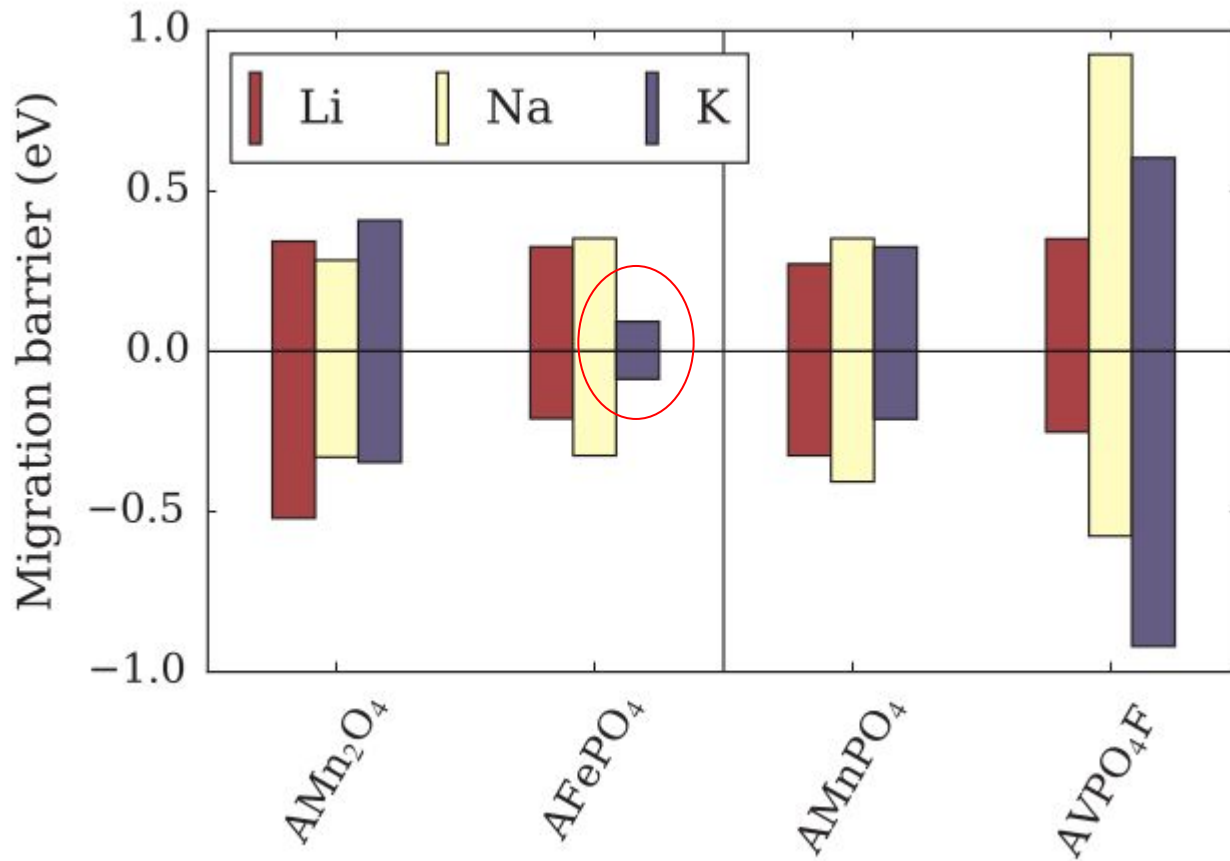
Origin of migration barriers

- What is the origin of migration barrier in cathode materials ?
- Is there any difference between Li, Na and K migration?



					
Ionic radius (Å)	0.78	0.97	1.33	1.48	1.45

Migration barriers with NEB method



Intercalated state -
Vacancy migration

Deintercalated state -
interstitial migration

Local contributions to migration barrier

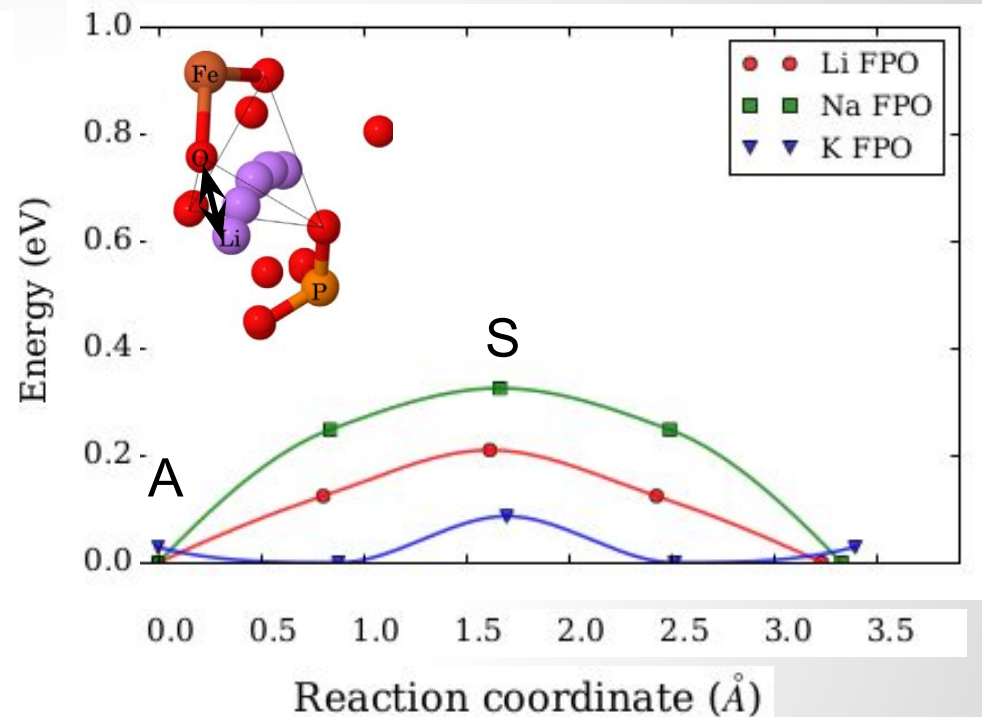
$$E_{\text{DFT}} = E_{\text{site}} + E_{\text{lattice}} - \text{approximately}$$

$$E_{\text{site}} = \sum Z_i/R_i + \sum \lambda_i \exp(-R_i/\rho_i)$$

- R_i - distance between each cation and migrating cation
- site electrostatic energy based on effective charges and Ewald summation
- λ_i and ρ_i are parameters for short range Born-Mayer repulsive interaction [Kunz1992]

$$dE_{\text{DFT}} = E(\text{S, DFT}) - E(\text{A, DFT})$$

$$dE_m = E_m(\text{S}) - E_m(\text{A})$$

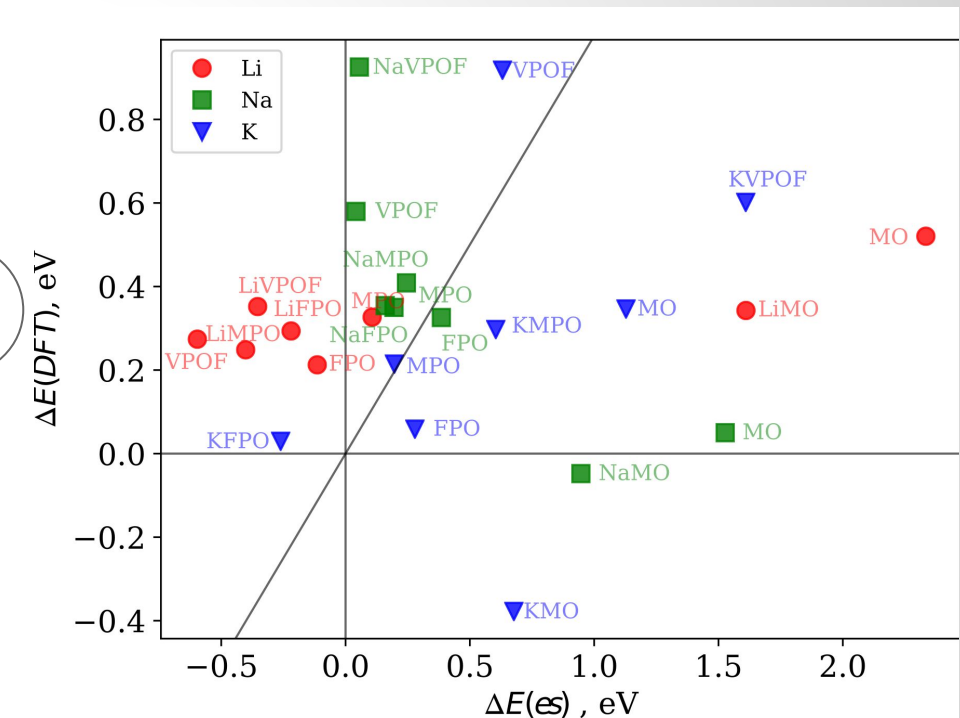
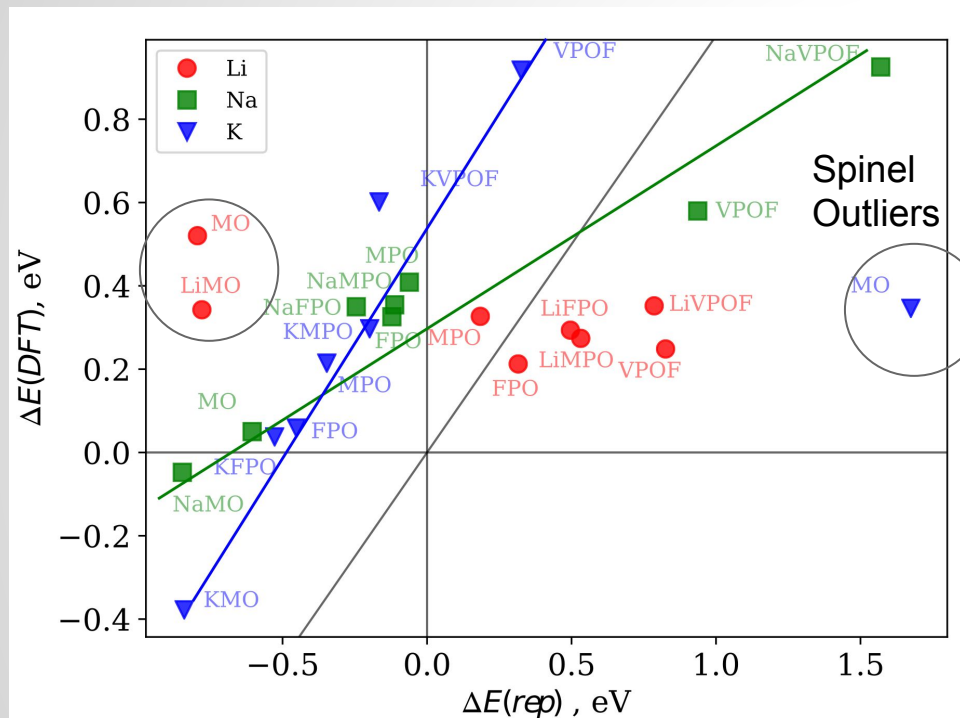


For many cases it is equivalent to migration barrier

Repulsive and electrostatic site energy

Change of repulsive energy vs dE(DFT)

Change of ES energy vs dE(DFT)

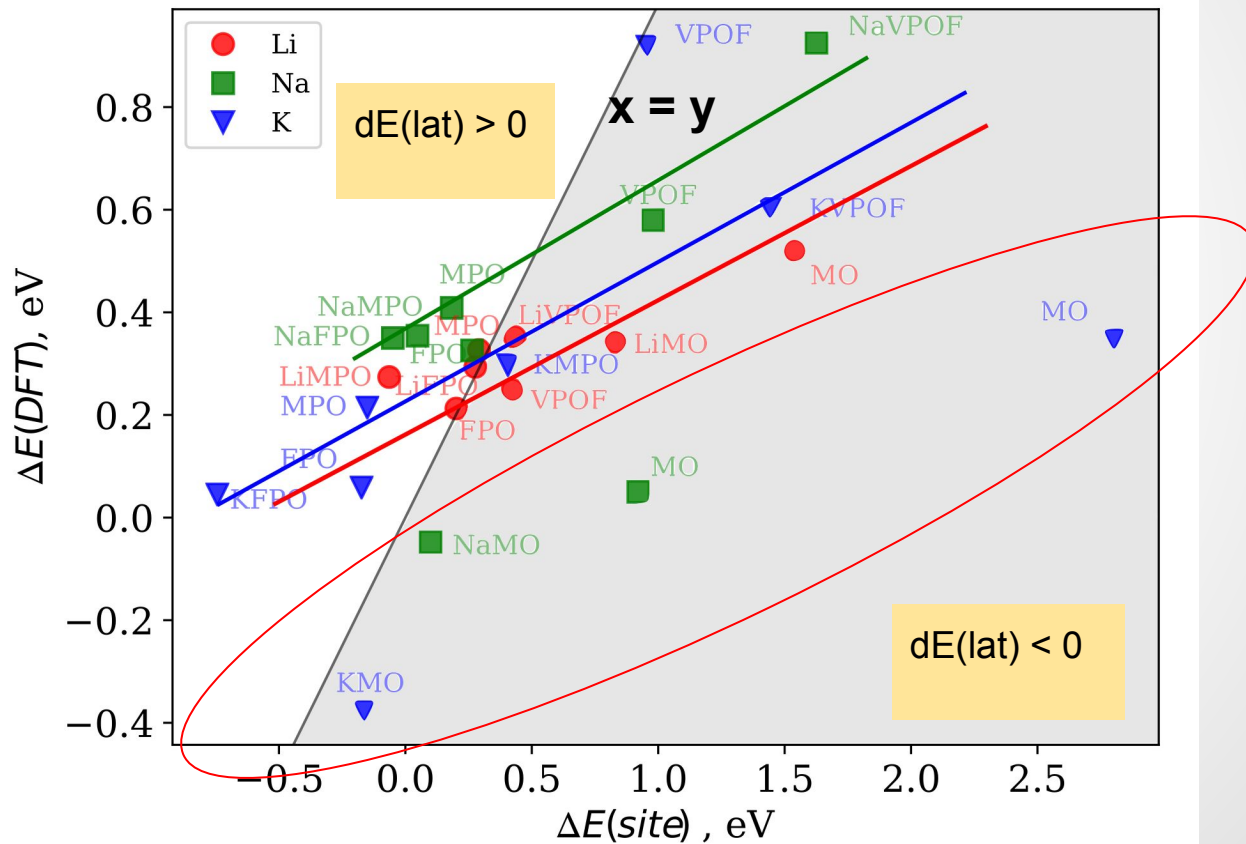


For K (MO omitted) and Na proportionality can be identified $R^2 = 0.6$

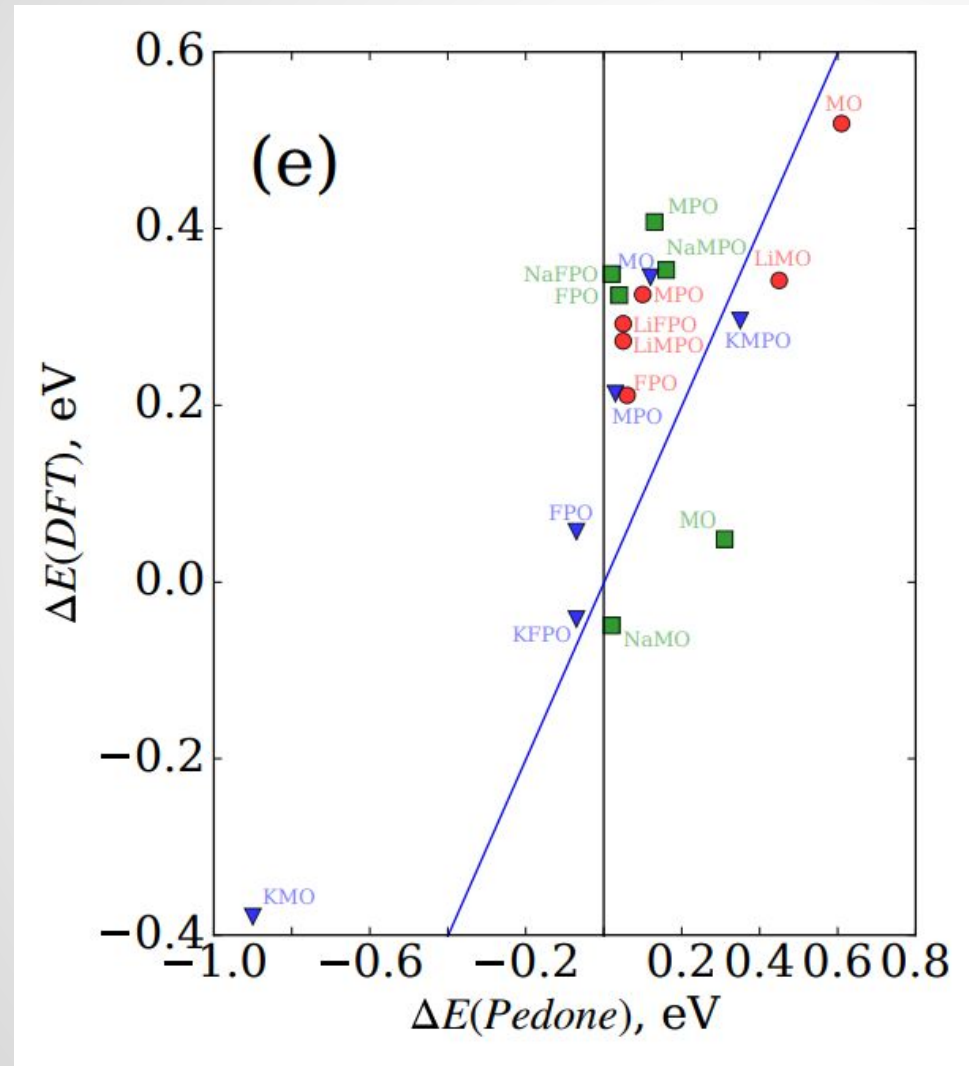
No correlation at all

Sum of repulsive and ES term vs dE (DFT)

$$\Delta E_{\text{lattice}} = \Delta E_{\text{DFT}} - \Delta E_{\text{site}}$$



Classical Interatomic potentials, $\Delta E_{\text{site}} + \Delta E_{\text{lattice}}$ (Pedone)



- Without potential parametrization, $R^2 = 0.6$
- Good quantitative description
- Spinel outliers are on line
- The lattice contribution is responsible for reducing energy at saddle point

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Thank you for your attention!